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## Nomenclature

|            |  |          |   |
|------------|--|----------|---|
| $A$        | fuselage cross-sectional area  | $K_{FI}$ | frame stiffness coefficient, $I_F/A_F^2$                              |
| $A_B$      | fuselage surface area  | $K_{mg}$ | shell minimum gage factor   |
| $A_F$      | frame cross-sectional area   | $K_P$    | shell geometry factor for hoop stress                                 |
| $(AR)$     | aspect ratio of wing   | $K_S$    | constant for shear stress in wing                                     |
| $b$        | wingspan; intercept of regression line                               | $K_{th}$ | sandwich thickness parameter  |
| $b_s$      | stiffener spacing  | $l_B$    | fuselage length   |
| $b_S$      | wing structural semispan, measured along quarter chord from fuselage | $l_{LE}$ | length from leading edge to structural box at theoretical root chord  |
| $b_w$      | stiffener depth  | $l_{MG}$ | length from nose to fuselage mounted main gear                        |
| $C_F$      | Shanley's constant   | $l_{NG}$ | length from nose to nose gear   |
| $C_P$      | center of pressure   | $l_{TE}$ | length from trailing edge to structural box at theoretical root chord |
| $C_R$      | root chord of wing at fuselage intersection                          | $l_1$    | length of nose portion of fuselage                                    |
| $C'_R$     | theoretical root chord of wing                                       | $l_2$    | length of tail portion of fuselage                                    |
| $C_{s1}$   | portion of wing leading edge not used for structural box             | $l_\pi$  | length from nose to breakpoint of fuselage                            |
| $C_{s2}$   | portion of wing trailing edge not used for structural box            | $L$      | lift  |
| $C_{SR}$   | structural root chord of wing  | $L_T$    | maximum vertical tail lift  |
| $C_{ST}$   | structural tip chord of wing   | $m$      | buckling equation exponent; slope of regression line                  |
| $C_T$      | tip chord of wing  | $M$      | longitudinal bending moment   |
| $d$        | frame spacing  | $n$      | normal load factor  |
| $d_W$      | optimum web spacing of wing  | $n_x$    | longitudinal acceleration   |
| $D$        | maximum diameter of fuselage   | $N_{xA}$ | axial stress resultant  |
| $e$        | wing buckling exponent   | $N_{xB}$ | bending stress resultant  |
| $e_C$      | wing cover material factor   | $N_{xP}$ | pressure stress resultant   |
| $E$        | Young's modulus of shell material                                    | $N_x^+$  | tensile axial stress resultant  |
| $E_F$      | Young's modulus of frame material                                    | $N_x^-$  | compressive axial stress resultant                                    |
| $F_{cy}$   | compressive yield strength   | $N_y$    | hoop direction stress resultant                                       |
| $F_S$      | shear strength   | $P$      | perimeter   |
| $F_{tu}$   | ultimate tensile strength  | $P_g$    | internal gage pressure  |
| $h$        | thickness of sandwich shell  | $P_s$    | perimeter of shell  |
| $h_{e_i}$  | step function for $i^{\text{th}}$ engine on wing                     | $P_w$    | perimeter of walls  |
| $h_{lg_i}$ | step function for $i^{\text{th}}$ landing gear on wing               | $P_1$    | exponent of power law of nose section of fuselage                     |
| $I_F$      | frame cross-sectional area moment of inertia                         | $P_2$    | exponent of power law of tail section of fuselage                     |
| $I_y$      | area moment of inertia about the y-axis                              | $r$      | radius of fuselage  |
| $I'_y$     | $I_y/\bar{t}_s$  |          |   |

|                |  |                |  |
|----------------|--|----------------|--|
| $r(y)$         | total wing chord as a function of position along quarter chord                     | $\bar{t}_{SC}$ | shell thickness required to preclude compressive failure             |
| $r_s(y)$       | structural wing chord as a function of position along quarter chord                | $\bar{t}_{SG}$ | shell thickness required to meet minimum gage constraint             |
| $R$            | correlation coefficient used for regression  | $\bar{t}_{ST}$ | shell thickness required to preclude tensile failure                 |
| $R_{fin}$      | fineness ratio   | $\bar{t}_T$    | smeared tension tie thickness  |
| $R_{HT}$       | ratio of horizontal tail station to fuselage length                                | $\bar{t}_w$    | smeared wall thickness   |
| $R_{LE}$       | ratio of wing leading edge station at theoretical root chord to fuselage length    | $\bar{t}_{wG}$ | thickness of wall to meet minimum gage constraint                    |
| $R_{MG}$       | ratio of length to main gear to fuselage length                                    | $\bar{t}_{wT}$ | thickness of wall required to prevent tensile failure                |
| $R_{NG}$       | ratio of length to nose gear to fuselage length                                    | $T$            | torque on wing carrythrough structure                                |
| $R_{P_1}$      | ratio of length to leading edge of fuselage mounted propulsion to fuselage length  | $V_B$          | fuselage volume  |
| $R_{P_2}$      | ratio of length to trailing edge of fuselage mounted propulsion to fuselage length | $V_W$          | volume of wing structural box, including structural components       |
| $R_t(y)$       | thickness ratio of wing as a function of position along quarter chord              | $V_1$          | volume of nose section of fuselage                                   |
| $R_{TAP}$      | taper ratio of wing  | $V_2$          | volume of tail section of fuselage                                   |
| $S_B$          | plan area of the fuselage  | $w_C$          | width of carrythrough structure of wing                              |
| $S_{LG}$       | stroke of landing gear   | $W$            | weight of aircraft structure   |
| $S_P$          | plan area of wing  | $W'$           | weight of wing per unit span   |
| $t(y)$         | thickness of wing box as a function of position along quarter chord                | $W_B$          | weight of fuselage structure and attached components                 |
| $t_c$          | core thickness   | $W_{FT}$       | weight of fuel   |
| $t_f$          | face sheet thickness   | $W_I$          | ideal fuselage structural weight                                     |
| $t_g$          | material gage thickness, $\bar{t}_s / K_{mg}$                                      | $W_{NO}$       | weight of nonoptimum material  |
| $t_{mg}$       | material minimum gage thickness  | $W_S$          | vehicle longitudinal weight distribution                             |
| $t_s$          | skin thickness   | $W_{TO}$       | gross takeoff weight of aircraft                                     |
| $t_w$          | stiffener thickness  | $W/S$          | shell structural weight per unit surface area                        |
| $\bar{t}$      | total equivalent isotropic thickness of shell and frames                           | $x$            | longitudinal fuselage coordinate                                     |
| $\bar{t}_B$    | total equivalent isotropic thickness of fuselage structure                         | $x_{calc}$     | weight calculated by PDCYL   |
| $\bar{t}_F$    | smeared equivalent isotropic thickness of frames                                   | $x_{HT}$       | distance from nose to theoretical quarter chord of horizontal tail   |
| $\bar{t}_S$    | equivalent isotropic thickness of shell  | $x_{LE}$       | distance from nose to leading edge of wing at theoretical root chord |
| $\bar{t}_{SB}$ | shell thickness required to preclude buckling failure                              | $x_{P_1}$      | distance from nose to leading edge of fuselage mounted propulsion    |
|                |  | $x_{P_2}$      | distance from nose to trailing edge of fuselage mounted propulsion   |

|              |  |              |  |
|--------------|--|--------------|--|
| $y$          | transverse fuselage coordinate; wing coordinate measured along quarter chord | $\epsilon_W$ | wing web structural efficiency                     |
| $y_{act}$    | actual weight  | $\Lambda$    | wing sweep   |
| $y_{est}$    | estimated weight after regression  | $\mu$        | wing loading                                       |
| $z$          | vertical fuselage coordinate   | $\rho$       | structural material density                        |
| $Z(y)$       | total width of wing box as a function of position along quarter chord        | $\rho_B$     | gross fuselage density                             |
| $Z_S(y)$     | width of wing box structure as a function of position along quarter chord    | $\rho_F$     | frame structural material density                  |
| $\delta$     | frame deflection   | $\sigma_S$   | allowable shear stress for wing                    |
| $\epsilon$   | shell buckling efficiency  | $\Sigma$     | sum over fuselage or wing length; solidity of wing |
| $\epsilon_C$ | wing cover structural efficiency   | $\psi$       | truss core angle                                   |

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## Summary

A method of estimating the load-bearing fuselage weight and wing weight of transport aircraft based on fundamental structural principles has been developed. This method of weight estimation represents a compromise between the rapid assessment of component weight using empirical methods based on actual weights of existing aircraft, and detailed, but time-consuming, analysis using the finite element method. The method was applied to eight existing subsonic transports for validation and correlation. Integration of the resulting computer program, PDCYL, has been made into the weights-calculating module of the AirCRAFT SYNThesis (ACSYNT) computer program. ACSYNT has traditionally used only empirical weight estimation methods; PDCYL adds to ACSYNT a rapid, accurate means of assessing the fuselage and wing weights of unconventional aircraft. PDCYL also allows flexibility in the choice of structural concept, as well as a direct means of determining the impact of advanced materials on structural weight.

Using statistical analysis techniques, relations between the load-bearing fuselage and wing weights calculated by PDCYL and corresponding actual weights were determined. A User's Manual and two sample outputs, one for a typical transport and another for an advanced concept vehicle, are given in the appendices.

## Introduction

A methodology based on fundamental structural principles has been developed to estimate the load-carrying weight of the fuselage and basic box weight of the wing for aircraft, and has been incorporated into the AirCRAFT SYNThesis program (ACSYNT). This weight routine is also available to run independently of ACSYNT, and is a modification of a collection of previously developed structural programs (refs. 1–4). The main subroutine called by ACSYNT is PDCYL. This study has concentrated on modern transport aircraft

because of the detailed weight information available, allowing the weights output from PDCYL to be compared to actual structural weights. The detailed weight statements also allow *nonoptimum* factors to be computed which, when multiplied by the load-bearing structural weights calculated by PDCYL, will give good representative total structure weight estimates. These nonoptimum factors will be computed through a regression analysis of a group of eight transport aircraft.

PDCYL is able to model both skin-stringer-frame and composite sandwich shell fuselage and wing box constructions. Numerous modifications were made to PDCYL and its associated collection of subroutines. These modifications include the addition of detailed fuselage shell geometry calculations; optional integration of a cylindrical fuselage midsection between the nose and tail sections; addition of landing and bump maneuvers to the load cases sizing the fuselage; ability to introduce an elliptical spanwise lift load distribution on the wing; variation of wing thickness ratio from tip to root; ability to place landing gear on the wing to relieve spanwise bending loads; distribution of propulsion system components between wing and fuselage; and the determination of maximum wingtip deflection.

## Brief Description of ACSYNT

The Aircraft Synthesis Computer program, ACSYNT, is an integrated design tool used in the modeling of advanced aircraft for conceptual design studies (ref. 5). ACSYNT development began at NASA Ames Research Center in the 1970s and continues to this day. The ACSYNT program is quite flexible and can model a wide range of aircraft configurations and sizes, from remotely piloted high altitude craft to the largest transport.

The ACSYNT program uses the following modules, not necessarily in this order: Geometry, Trajectory, Aerodynamics, Propulsion, Stability, Weights, Cost, Advanced Aerodynamic Methods, and Takeoff. An ACSYNT run would normally progress as follows: the Geometry module is called to define the aircraft shape and configuration; the Trajectory module then runs the vehicle through a specified mission; finally the Weight and Cost

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modules are executed. To determine the performance of the vehicle at each mission point, the Trajectory module will call the Aerodynamics and Propulsion modules.

After the mission is completed, the calculated weight of the aircraft may be compared with the initial estimate and an iteration scheme run to converge upon the required aircraft weight. This process is necessarily iterative as the aircraft weight ACSYNT calculates is dependent upon the initial weight estimate.

ACSYNT is able to perform a *sensitivity analysis* on any design variable, such as aspect ratio, thickness-to-chord ratio, fuselage length or maximum fuselage diameter. Sensitivity is defined as (change in objective function/value of objective function) divided by (change in design variable/design variable). As an example, if gross weight is the objective function and decreases when the wing thickness-to-chord ratio increases, then the sensitivity of thickness-to-chord ratio is negative. It is important to note that while this increase in thickness-to-chord ratio lowers the gross weight of the aircraft, it may also have a detrimental effect on aircraft performance.

ACSYNT is also able to size multiple design variables by optimizing the objective function. The objective function represents the interactions between design disciplines such as structures, aerodynamics and propulsion. The automated sizing of design variables during the optimization process is accomplished using the gradient method. Two types of constraints may be imposed during the optimization process. These are performance-based constraints such as runway length or maximum roll angle, and side constraints on design variables such as limitations on wing span or fuselage length. ACSYNT never violates constraints during the optimization process so that each iteration produces a valid aircraft.

### Methods of Weight Estimation

Two methods are commonly available to estimate the load-bearing fuselage weight and wing box structure weight of aircraft. These methods, in increasing order of complexity and accuracy, are empirical regression and detailed finite element structural analysis. Each method has particular advantages and limitations which will be briefly discussed in the following sections. There is an additional method based on classical plate theory (CPT) which may be used to estimate the weight of the wing box structure.

**Empirical**– The empirical approach is the simplest weight estimation tool. It requires knowledge of fuselage and wing weights from a number of similar existing aircraft in addition to various key configuration parameters of these aircraft in order to produce a linear regres-

sion. This regression is a function of the configuration parameters of the existing aircraft and is then scaled to give an estimate of fuselage and wing weights for an aircraft under investigation. Obviously, the accuracy of this method is dependent upon the quality and quantity of data available for existing aircraft. Also, the accuracy of the estimation will depend on how closely the existing aircraft match the configuration and weight of the aircraft under investigation. All of the empirical regression functions currently in the ACSYNT program give total fuselage weight and total wing weight.

**Finite Element**– Finite element analysis is the matrix method of solution of a discretized model of a structure. This structure, such as an aircraft fuselage or wing, is modeled as a system of elements connected to adjacent elements at nodal points. An element is a discrete (or finite) structure that has a certain geometric makeup and set of physical characteristics. A nodal force acts at each nodal point, which is capable of displacement. A set of mathematical equations may be written for each element relating its nodal displacements to the corresponding nodal forces. For skeletal structures, such as those composed of rods or beams, the determination of element sizing and corresponding nodal positioning is relatively straightforward. Placement of nodal points on these simple structures would naturally fall on positions of concentrated external force application or joints, where discontinuities in local displacement occur.

Continuum structures, such as an aircraft fuselage or wing, which would use some combination of solid, flat plate, or shell elements, are not as easily discretizable. An approximate mesh of elements must be made to model these structures. In effect, an idealized model of the structure is made, where the element selection and sizing is tailored to local loading and stress conditions.

The assembly of elements representing the entire structure is a large set of simultaneous equations that, when combined with the loading condition and physical constraints, can be solved to find the unknown nodal forces and displacements. The nodal forces and displacements are then substituted back into the each element to produce stress and strain distributions for the entire structural model.

**Classical Plate Theory**– CPT has been applied to wing structure design and weight estimation for the past 20 years. Using CPT a mathematical model of the wing based on an equivalent plate representation is combined with global Ritz analysis techniques to study the structural response of the wing. An equivalent plate model does not require detailed structural design data as required for finite element analysis model generation and has been shown to be a reliable model for low aspect ratio fighter

wings. Generally, CPT will overestimate the stiffness of more flexible, higher aspect ratio wings, such as those employed on modern transport aircraft. Recently, transverse shear deformation has been included in equivalent plate models to account for this added flexibility. This new technique has been shown to give closer representations of tip deflection and natural frequencies of higher aspect ratio wings, although it still overestimates the wing stiffness. No fuselage weight estimation technique which corresponds to the equivalent plate model for wing structures is available.

### **Need for Better, Intermediate Method**

Preliminary weight estimates of aircraft are traditionally made using empirical methods based on the weights of existing aircraft, as has been described. These methods, however, are undesirable for studies of unconventional aircraft concepts for two reasons. First, since the weight estimating formulas are based on existing aircraft, their application to unconventional configurations (i.e., canard aircraft or area ruled bodies) is suspect. Second, they provide no straightforward method to assess the impact of advanced technologies and materials (i.e., bonded construction and advanced composite laminates).

On the other hand, finite-element based methods of structural analysis, commonly used in aircraft detailed design, are not appropriate for conceptual design, as the idealized structural model must be built off-line. The solution of even a moderately complex model is also computationally intensive and will become a bottleneck in the vehicle synthesis. Two approaches which may simplify finite-element structural analysis also have drawbacks. The first approach is to create detailed analyses at a few critical locations on the fuselage and wing, then extrapolate the results to the entire aircraft, but this can be misleading because of the great variety of structural, load, and geometric characteristics in a typical design. The second method is to create an extremely coarse model of the aircraft, but this scheme may miss key loading and stress concentrations in addition to suffering from the problems associated with a number of detailed analyses.

The fuselage and wing structural weight estimation method employed in PDCYL is based on another approach, beam theory structural analysis. This results in a weight estimate that is directly driven by material properties, load conditions, and vehicle size and shape, and is not confined to an existing data base. Since the analysis is done station-by-station along the vehicle longitudinal axis, and along the wing structural chord, the distribution of loads and vehicle geometry is accounted for, giving an integrated weight that accounts for local conditions. An analysis based solely on fundamental

principles will give an accurate estimate of structural weight only. Weights for fuselage and wing secondary structure, including control surfaces and leading and trailing edges, and some items from the primary structure, such as doublers, cutouts, and fasteners, must be estimated from correlation to existing aircraft.

The equivalent plate representation, which is unable to model the fuselage structure, is not used in PDCYL.

## **Methods**

### **Overview**

Since it is necessary in systems analysis studies to be able to rapidly evaluate a large number of specific designs, the methods employed in PDCYL are based on idealized vehicle models and simplified structural analysis. The analyses of the fuselage and wing structures are performed in different routines within PDCYL, and, as such, will be discussed separately. The PDCYL weight analysis program is initiated at the point where ACSYNT performs its fuselage weight calculation. PDCYL first performs a basic geometrical sizing of the aircraft in which the overall dimensions of the aircraft are determined and the propulsion system, landing gear, wing, and lifting surfaces are placed.

**Fuselage**—The detailed fuselage analysis starts with a calculation of vehicle loads on a station-by-station basis. Three types of loads are considered—longitudinal acceleration (applicable to high-thrust propulsion systems), tank or internal cabin pressure, and longitudinal bending moment. All of these loads occur simultaneously, representing a critical loading condition. For longitudinal acceleration, longitudinal stress resultants caused by acceleration are computed as a function of longitudinal fuselage station; these stress resultants are compressive ahead of the propulsion system and tensile behind the propulsion system. For internal pressure loads, the longitudinal distribution of longitudinal and circumferential (hoop) stress resultants is computed for a given shell gage pressure (generally 12 psig). There is an option to either use the pressure loads to reduce the compressive loads from other sources or not to do this; in either case, the pressure loads are added to the other tensile loads.

Longitudinal bending moment distributions from three load cases are examined for the fuselage. Loads on the fuselage are computed for a quasi-static pull-up maneuver, a landing maneuver, and travel over runway bumps. These three load cases occur at user-specified fractions of gross takeoff weight. Aerodynamic loads are computed as a constant fraction of fuselage planform area and are considered negligible for subsonic transports. For



pitch control there is an option to use either elevators mounted on the horizontal tail (the conventional configuration) or elevons mounted on the trailing edges of the wing. The envelope of maximum bending moments is computed for all three load cases and is then used to determine the net stress resultants at each fuselage station.

After the net stress resultants are determined at each fuselage station, a search is conducted at each station to determine the amount of structural material required to preclude failure in the most critical condition at the most critical point on the shell circumference. This critical point is assumed to be the outermost fiber at each station. Failure modes considered are tensile yield, compressive yield, local buckling, and gross buckling of the entire structure. A minimum gage restriction is also imposed as a final criterion. It is assumed that the material near the neutral fiber of the fuselage (with respect to longitudinal bending loads) is sufficient to resist the shear and torsion loads transmitted through the fuselage. For the shear loads this is a good approximation as the fibers farthest from the neutral axis will carry no shear. Also, for beams with large fineness ratios (fuselage length/maximum diameter) bending becomes the predominant failure mode.

The maximum stress failure theory is used for predicting yield failures. Buckling calculations assume stiffened shells behave as wide columns and sandwich shells behave as cylinders. The frames required for the stiffened shells are sized by the Shanley criterion. This criterion is based on the premise that, to a first-order approximation, the frames act as elastic supports for the wide column (ref. 6).

There are a variety of structural geometries available for the fuselage. There is a simply stiffened shell concept using longitudinal frames. There are three concepts with Z-stiffened shells and longitudinal frames; one with structural material proportioned to give minimum weight in buckling, one with buckling efficiency compromised to give lighter weight in minimum gage, and one a buckling-pressure compromise. Similarly, there are three truss-core sandwich designs, two for minimal weight in buckling with and without frames, and one a buckling-minimum gage compromise.

It is assumed that the structural materials exhibit elastoplastic behavior. Further, to account for the effects of creep, fatigue, stress-corrosion, thermal cycling and thermal stresses, options are available to scale the material properties of strength and Young's modulus of elasticity. In the numerical results of this study, all materials were considered elastic and the full room-temperature material properties were used.

Composite materials can be modeled with PDCYL by assuming them to consist of orthotropic lamina formed into quasi-isotropic (two-dimensionally, or planar, isotropic) laminates. Each of the lamina is assumed to be composed of filaments placed unidirectionally in a matrix material. Such a laminate has been found to give very nearly minimum weight for typical aircraft structures.

**Wing**– The wing structure is a multi-web box beam designed by spanwise bending and shear. The wing-fuselage carrythrough structure, defined by the wing-fuselage intersection, carries the spanwise bending, shear, and torsion loads introduced by the outboard portion of the wing.

The load case used for the wing weight analysis is the quasi-static pull-up maneuver. The applied loads to the wing include the distributed lift and inertia forces, and the point loads of landing gear and propulsion, if placed on the wing. Fuel may also be stored in the wing, which will relieve bending loads during the pull-up maneuver.

The wing weight analysis proceeds in a similar fashion to that of the fuselage. The weight of the structural box is determined by calculating the minimum amount of material required to satisfy static buckling and strength requirements at a series of spanwise stations. The covers of the multi-web box are sized by buckling due to local instability and the webs by flexure-induced crushing. Required shear material is computed independently of buckling material. Aeroelastic effects are not accounted for directly, although an approximation of the magnitude of the tip deflection during the pull-up maneuver is made. For the carrythrough structure, buckling, shear, and torsion material are computed independently and summed.

As for the fuselage, there are a variety of structural geometries available. There are a total of six structural concepts, three with unstiffened covers and three with truss-stiffened covers. Both cover configurations use webs that are either Z-stiffened, unflanged, or trusses.

## Geometry

**Fuselage**– The fuselage is assumed to be composed of a nose section, an optional cylindrical midsection, and a tail section. The gross density and fineness ratio are defined as

$$\rho_B = \frac{W_B}{V_B} \quad (1)$$

$$R_{fin} = \frac{l_B}{D} \quad (2)$$

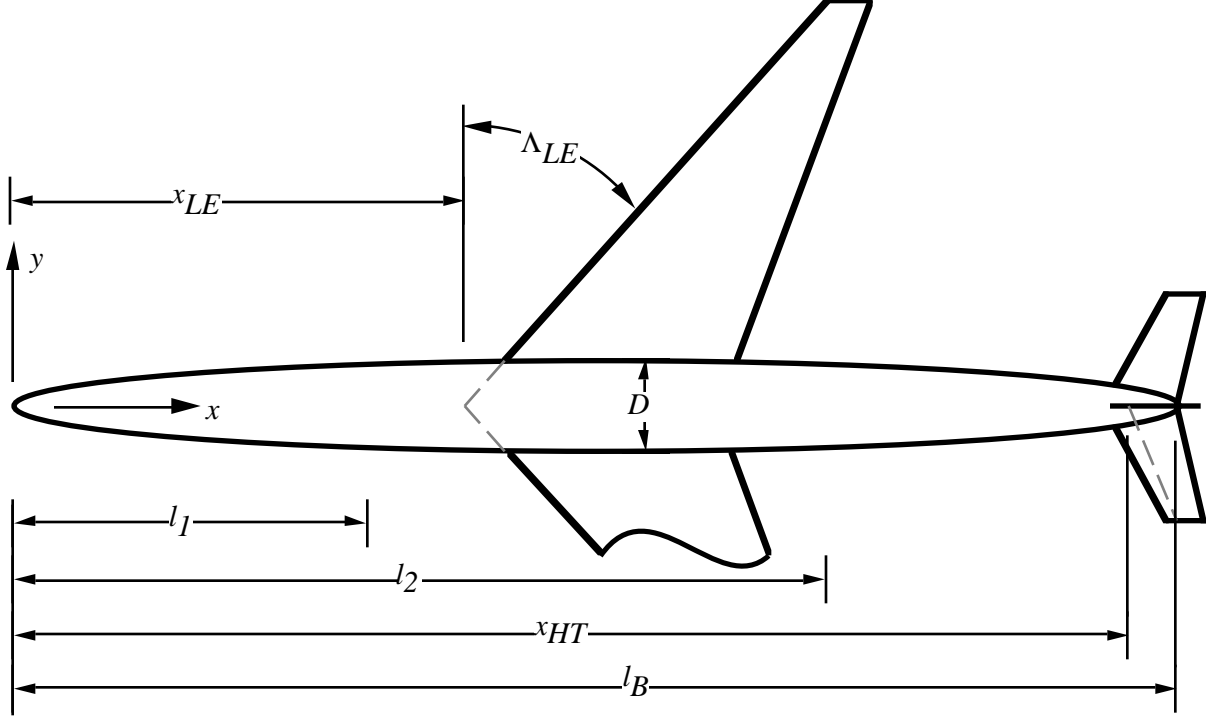


Figure 1. The body configuration.

where  $W_B$  is the fuselage weight ( $W_B =$  gross takeoff weight excluding the summed weight of the wing, tails, wing-mounted landing gear, wing-mounted propulsion, and fuel if stored in the wing),  $V_B$  is the total fuselage volume,  $l_B$  is the fuselage length, and  $D$  is the maximum fuselage diameter. The fuselage outline is defined by two power-law bodies of revolution placed back-to-back, with an optional cylindrical midsection between them (fig. 1). (For the present study, all eight transports used for validation of the analysis used the optional cylindrical midsection.)

With the cylindrical midsection, integration gives the fuselage volume, fuselage planform area, and fuselage surface area as

$$V_B = \frac{\pi D^2}{4} \left[ \frac{l_1}{2P_1 + 1} + (l_B - l_2 - l_1) + \frac{l_2}{2P_2 + 1} \right] \quad (3)$$

$$S_B = D \left[ \frac{l_1}{P_1 + 1} + (l_B - l_2 - l_1) + \frac{l_2}{P_2 + 1} \right] \quad (4)$$

$$A_B = \pi S_B \quad (5)$$

respectively, where  $l_1$  and  $l_2$  are the respective lengths to the start and end of the cylindrical midsection, and  $P_1$  and  $P_2$  are the respective powers that describe the nose and tail sections.  $P_1$  and  $P_2$ , again for the case of the cylindrical midsection, are found by solving the power-law

equations for the volumes of the nose and tail sections, which are input from ACSYNT. The solution of these equations gives the respective nose and tail powers as

$$P_1 = \frac{\pi D^2 l_1}{8V_1} - \frac{1}{2} \quad (6)$$

$$P_2 = \frac{\pi D^2 l_2}{8V_2} - \frac{1}{2} \quad (7)$$

where  $V_1$  and  $V_2$  are the corresponding nose and tail volumes.

The horizontal tail is placed according to its quarter chord location as a fraction of the fuselage length. The distance from the nose to the tail is

$$x_{HT} = l_B R_{HT} \quad (8)$$

where  $R_{HT}$  is the ratio of horizontal tail station to fuselage length.

Propulsion may be either mounted on the fuselage or placed on the wing. In the case of fuselage mounted propulsion, the starting and ending positions of the propulsion unit are again calculated from their respective fractions of fuselage length as

$$x_{P_1} = l_B R_{P_1} \quad (9)$$

$$x_{P_2} = l_B R_{P_2} \quad (10)$$

where  $R_{P1}$  and  $R_{P2}$  are the corresponding ratios of lengths to the leading and trailing edges of the fuselage engine pod to fuselage length.

Similarly, the nose landing gear is placed on the fuselage as a fraction of vehicle length; the main gear, on the other hand, may be placed either on the fuselage as a single unit, also as a fraction of fuselage length, or on the wing in multiple units as will be described below. The positions of the respective nose and optional fuselage-mounted main gear are

$$l_{NG} = l_B R_{NG} \quad (11)$$

$$l_{MG} = l_B R_{MG} \quad (12)$$

where  $R_{NG}$  and  $R_{MG}$  are the corresponding length ratios for the nose gear and main gear stations to vehicle length.

**Wing**– The lifting planforms are assumed to be tapered, swept wings with straight leading and trailing edges. The planform shape is trapezoidal as the root chord and tip chord are parallel.

The wing loading is defined as

$$\mu = \frac{W_{TO}}{S_P} \quad (13)$$

where  $S_P$  is the wing planform area.

The wing is placed on the fuselage according to the location of the leading edge of its root chord, determined as a fraction of the fuselage length. The distance from the nose to the leading edge of the wing is

$$x_{LE} = l_B R_{LE} \quad (14)$$

where  $R_{LE}$  is the ratio of leading edge station to fuselage length.

The first step in computing the wing weight is the determination of the geometry of the structural wing box. In terms of the input parameters  $W_{TO}$ ,  $(W/S_p)$ , aspect ratio ( $AR$ ), taper ratio ( $R_{TAP}$ ), and leading edge sweep ( $\Lambda_{LE}$ ), the dependent parameters wing area, span, root chord, tip chord, and trailing edge wing sweep are computed from

$$S_P = \frac{W_{TO}}{W/S} \quad (15)$$

$$b = \sqrt{(AR)S_P} \quad (16)$$

$$C'_R = \frac{2S_P}{b(1 + R_{TAP})} \quad (17)$$

$$C_T = R_{TAP}C'_R \quad (18)$$

$$\tan(\Lambda_{TE}) = \tan(\Lambda_{LE}) + \frac{2C'_R}{b}(R_{TAP} - 1) \quad (19)$$

(fig. 2). It is assumed that specified portions of the streamwise (aerodynamic) chord are required for controls and high lift devices, leaving the remainder for the structural wing box. The portions of the leading and trailing edges that are left for nonstructural use are specified as respective fractions  $C_{S1}$  and  $C_{S2}$  of the streamwise chord. Determination of these chord fractions is accomplished through visual inspection of the wing planform. Measured at the theoretical root chord, the dimensions for the leading and trailing edges are

$$l_{LE} = C_{S1}C'_R \quad (20)$$

$$l_{TE} = C_{S2}C'_R \quad (21)$$

respectively. The intersection of this structural box with the fuselage contours determines the location of the rectangular carrythrough structure. The width of the carrythrough structure,  $w_C$ , is defined by the corresponding fuselage diameter.

The dimensions of the structural box and of the carrythrough structure are now determined (fig. 3). The structural semispan,  $b_S$ , is assumed to lie on the quarter-chord line,  $y$ , whose sweep is given by

$$\tan(\Lambda_S) = \frac{3}{4}\tan(\Lambda_{LE}) + \frac{1}{4}\tan(\Lambda_{TE}) \quad (22)$$

Thus,

$$b_S = \frac{b - D}{2\cos(\Lambda_S)} \quad (23)$$

The streamwise chord at any point on the wing is given by

$$r(\zeta) = C'_R - \frac{\zeta}{b/2}(C'_R - C_T) \quad (24)$$

where  $\zeta$  is measured perpendicular to the vehicle longitudinal axis from the vehicle centerline toward the wingtip. Thus, the streamwise chord is the dimension of the wing parallel to the vehicle longitudinal axis. In particular, at the wing-fuselage intersection,

$$C_R = C'_R - \frac{D}{b}(C'_R - C_T) \quad (25)$$

The structural root and tip chords are

$$C_{SR} = (1 - C_{S1} - C_{S2})C_R \quad (26)$$

$$C_{ST} = (1 - C_{S1} - C_{S2})C_T \quad (27)$$

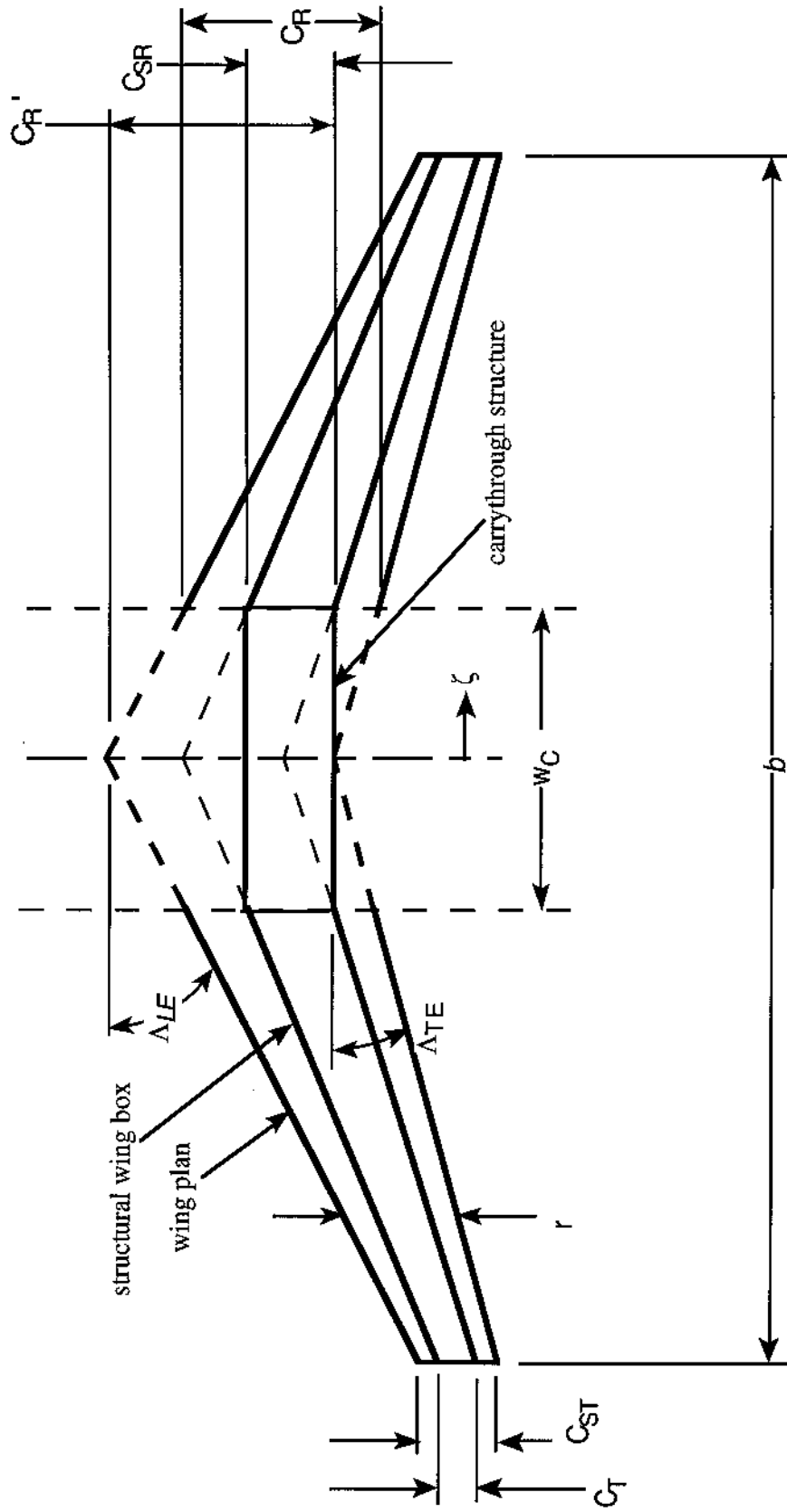


Figure 2. Wing structural planform geometry.

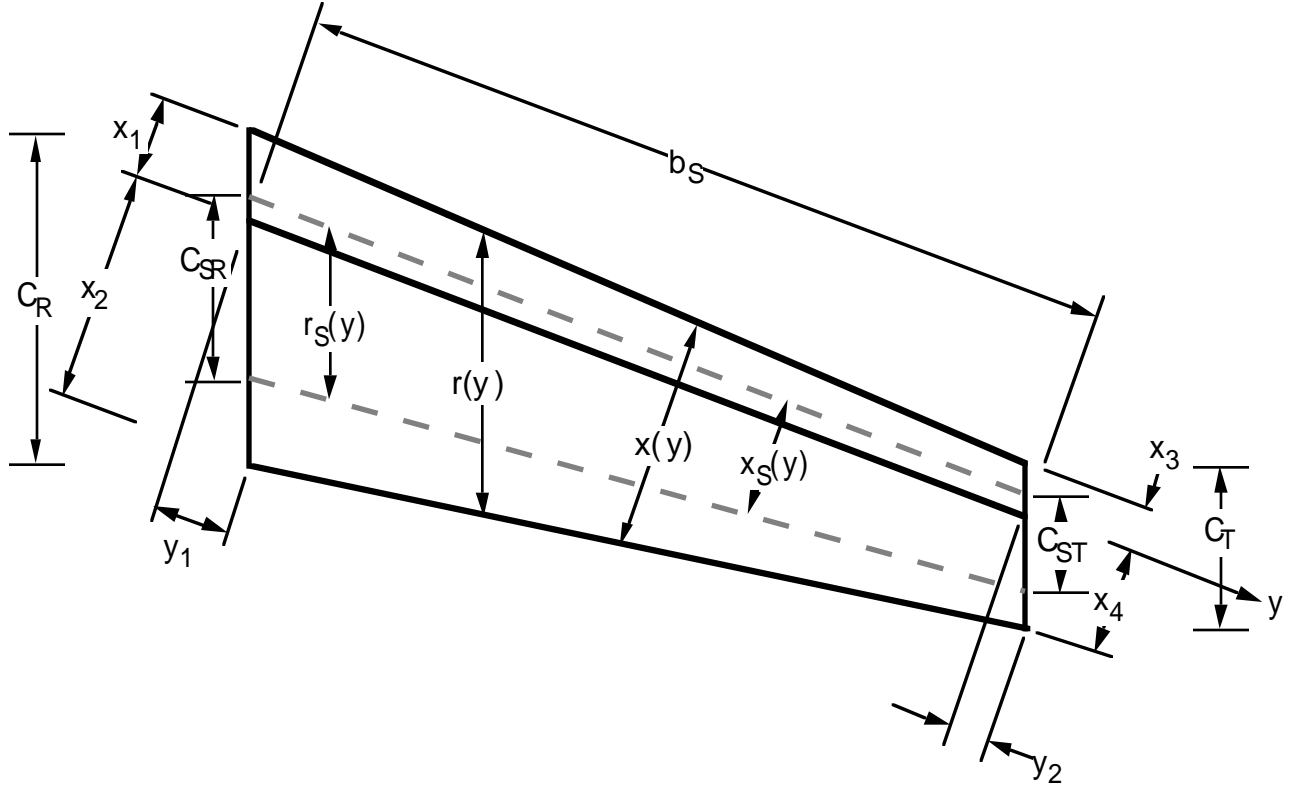


Figure 3. Wing coordinate system.

respectively. In terms of  $y$ , measured along the quarter chord from the wing-fuselage intersection toward the wingtip, the structural and total chords are given by

$$r_S(y) = C_{SR} - \frac{y}{b_S} (C_{SR} - C_{ST}) \quad (28)$$

$$r(y) = C_R - \frac{y}{b_S} (C_R - C_T) \quad (29)$$

where the structural chord is defined as the dimension of the rectangular-section wing box measured parallel to the vehicle longitudinal axis. Computation of the widths of the wing box and total wing structure, as shown in figure 3, is relatively complicated due to the geometry at the wingtip and the wing-fuselage intersection. For the portion of the wing between the wingtip and the wing-fuselage intersection, the respective widths of the wing box and total wing structure at any spanwise station  $y$  are

$$Z_S(y) = r_S \cos(\Lambda_S) \quad (30)$$

$$Z(y) = r \cos(\Lambda_S) \quad (31)$$

where  $Z_S(y)$  and  $Z(y)$  are dimensions perpendicular to the structural semispan.

The thickness of the wing box at any spanwise station  $y$  is determined as a linear interpolation between the root and tip thickness ratios multiplied by the chord at  $y$ .

$$t(y) = \begin{cases} rR_t(y), & 0 \leq y \leq b_S & \text{(box structure)} \\ rR_t(0), & y < 0 & \text{(carrythrough structure)} \end{cases} \quad (32)$$

where  $R_t(y)$  is the thickness ratio of the wing as a function of position along the quarter chord.

For the transports in the present study, all the fuel is carried within the wing structure. An option is also available to carry the fuel entirely within the fuselage, negating any bending relief in the wing. (The high altitude drone, described in Appendix B, was modeled with a fuselage fuel tank.) The volume of the trapezoidal planform, rectangular-section wing box structure (including the carrythrough structure) is found as follows:

$$\begin{aligned}
V_W &= 2 \int_0^{b_S} Z_S(y) t(y) dy + (1 - C_{S_1} - C_{S_2}) R_{t_R} C_{R}^2 w_C \\
&= 2 \cos(\Lambda_S) (1 - C_{S_1} - C_{S_2}) \\
&\quad \times \int_0^{b_S} \left[ C_R - \frac{y}{b_S} (C_R - C_T) \right] \\
&\quad \times \left[ R_{t_R} C_R - \frac{y}{b_S} (R_{t_R} C_R - R_{t_T} C_T) \right] dy \\
&\quad + (1 - C_{S_1} - C_{S_2}) R_{t_R} C_{R}^2 w_C \\
&= \frac{b_S (1 - C_{S_1} - C_{S_2}) \cos(\Lambda_S)}{3} \\
&\quad \times \left[ R_{t_R} C_R (2C_R + C_T) + R_{t_T} C_T (C_R + 2C_T) \right] \\
&\quad + (1 - C_{S_1} - C_{S_2}) R_{t_R} C_{R}^2 w_C
\end{aligned} \tag{33}$$

This equation is based on flat upper and lower surfaces and neglects the volume taken up by the structure.

## Loads

**Fuselage**– Fuselage loading is determined on a station-by-station basis along the length of the vehicle. Three types of fuselage loads are considered—longitudinal acceleration, tank pressure, and bending moment. In the present study, all three load types are assumed to occur simultaneously to determine maximum compressive and tensile loads at the outer shell fibers at each station.

Bending loads applied to the vehicle fuselage are obtained by simulating vehicle pitch-plane motion during a quasi-static pull-up maneuver; a landing; and movement over a runway bump. Simplified vehicle loading models are used where it is assumed that: (1) fuselage lift forces (nominally zero for subsonic transports) are distributed uniformly over the fuselage plan area; (2) wing loading, determined independently, is transferred by a couple of vertical force and torque through the wing carrythrough structure; (3) fuselage weight is distributed uniformly over fuselage volume; (4) control surface forces and landing gear reactions are point loads; and (5) the propulsion system weight, if mounted on the fuselage, is uniformly distributed. A factor of safety (nominally 1.5) is applied to each load case. The aircraft weight for each case is selected as a fraction of gross takeoff weight. The resulting one-dimensional loading model is shown in

figure 4. All fuselage lift forces are assumed to be linear functions of angle of attack. Longitudinal bending moments are computed for each of the three loading cases and the envelope of the maximum values taken as the design loading condition. The bending moment computation is given in detail in reference 4 and will only be summarized here.

Considering first the pull-up maneuver loading, the motion is assumed to be a quasi-static pitch-plane pull-up of given normal load factor  $n$  (nominally 2.5 for transport aircraft). The vehicle is trimmed with the appropriate control surface (a horizontal tail for all eight transport used for validation in the present study), after which the angle of attack is calculated.

Landing loads are developed as the aircraft descends at a given vertical speed,  $V_S$ , after which it impacts the ground; thereafter the main and nose landing gears are assumed to exert a constant, or optionally a  $(1 - \cos(\omega t))$ , force during its stroke,  $S_{LG}$ , until the aircraft comes to rest. The vehicle weight is set equal to the nominal landing weight. Wing lift as a fraction of landing weight is specified, which reduces the effective load the landing gear carries. Likewise, the portion of total vehicle load the main gear carries is specified. No pitch-plane motion is considered during the landing.

Runway bump loads are handled by inputting the bump load factor into the landing gear. Bump load factor is applied according to reference 7. This simulates the vehicle running over a bump during taxi. In a similar fashion to the landing, the wing lift as a fraction of gross takeoff weight is specified, as is the portion of effective load input through the main gear. No pitch-plane motion is considered during the bump.

**Wing**– For the wing, only a quasi-static pull-up maneuver condition at load factor  $n$  is considered for determining loads. At each spanwise station along the quarter chord, from the wingtip to the wing-fuselage intersection, the lift load, center of pressure, inertia load, center of gravity, shear force, and bending moment are computed. For the inertia load, it is assumed that the fuel weight  $W_{FT}$  is distributed uniformly with respect to the wing volume so that the inertial load at  $y$  is  $(W_{FT}/V_W) * V(y)$ , where  $V(y)$  is the volume outboard of  $y$ ; this volume has centroid  $C_g(y)$  with respect to station  $y$ . An estimate of the wing structural weight is included in  $W_{FT}$  for this calculation but the calculation is not redone when the actual structural weight has been computed.

There is an option for either a trapezoidal or a Schrenk (ref. 8) lift load distribution along the wingspan; the trapezoidal distribution represents a uniform lift over the wing area (which has a trapezoidal planform) while the

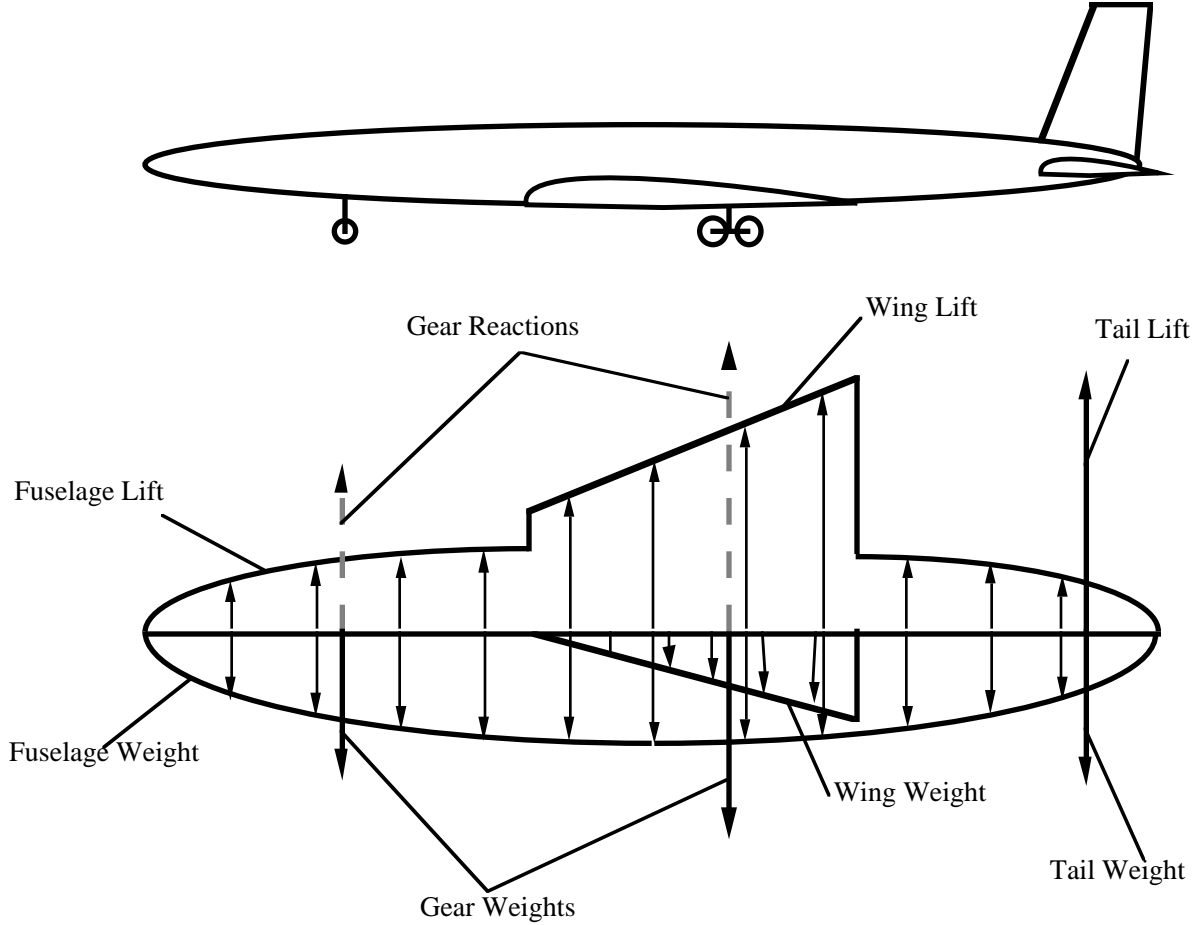


Figure 4. Loading model.

Schrenk distribution is an average of the trapezoidal distribution with an elliptical distribution, where the lift is zero at the wingtip and maximum at the wing-fuselage intersection. Prandtl has shown that a true elliptical lift load distribution will have a minimum induced drag, but a combination of the elliptical and trapezoidal distributions will give a better representation of actual aircraft loading (ref. 8).

Plots of trapezoidal and Schrenk lift load distributions are shown in figure 5. For the trapezoidal lift load distribution the lift load at  $y$  is  $(W/S)A_{TRAP}(y)$ , where  $A_{TRAP}(y)$  is the area outboard of  $y$ ; the centroid of this area is denoted  $C_{P_{TRAP}}(y)$ , where  $y$  is measured along the quarter chord. For the elliptical lift load distribution, the lift load matches the contour of an ellipse with the end of its major axis on the tip and the end of its minor axis directly above the wing-fuselage intersection. The area enclosed by the quadrant of the ellipse is set equal to the exposed area of the trapezoidal wing panel

$$S_{ELL} = \frac{(b - w_C)}{4} (1 + R_{TAP}) C_R \quad (34)$$

Thus the value of lift at  $y$ ,  $L_{ELL}$ , the area of ellipse outboard of  $y$ ,  $A_{ELL}$ , and the center of pressure of lift outboard of  $y$ ,  $C_{P_{ELL}}$ , for  $y$  measured along the structural box may be determined as

$$L_{ELL}(y) = \frac{4S_{ELL}}{\pi b_S} \left[ 1 - \left( \frac{y}{b_S} \right)^2 \right]^{\frac{1}{2}} \quad (35)$$

$$A_{ELL}(y) = S_{ELL}$$

$$- \left\{ \frac{2S_{ELL}}{\pi b_S^2} \left[ y(b_S^2 - y^2)^{\frac{1}{2}} + b_S^2 \sin^{-1} \left( \frac{y}{b_S} \right) \right] \right\} \quad (36)$$

$$C_{P_{ELL}}(y) = \frac{4}{3\pi} (b_S - y) \quad (37)$$

respectively.

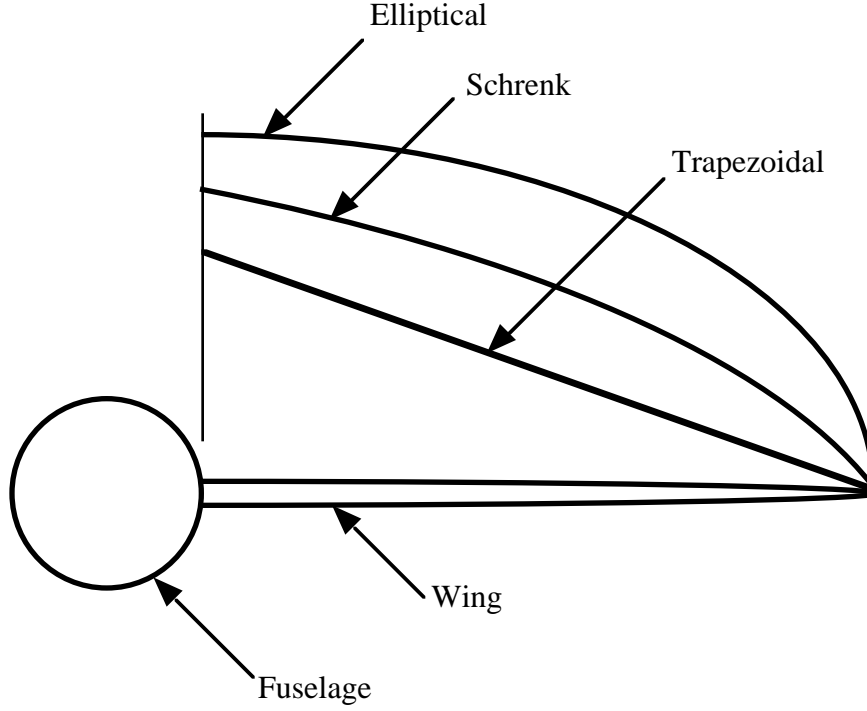


Figure 5. Trapezoidal and Schrenk lift load distributions.

For the Schrenk lift load distribution, the average of  $A_{TRAP}(y)$  and  $A_{ELL}(y)$  is used to represent the composite area, while the average of  $C_{P_{TRAP}}(y)$  and  $C_{P_{ELL}}(y)$  is used to represent the composite center of pressure.

Using the appropriate outboard area  $A(y)$  and center of pressure  $C_p(y)$ , the shear force is

$$F_S(y) = nK_S \left[ \frac{W}{S} A - \frac{W_{FT}}{V_W} V - \sum_{i=1}^{n_e} h_e(y_{e_i} - y) W_{e_i} - \sum_{i=1}^{n_{lg}} h_{lg}(y_{lg_i} - y) W_{lg_i} \right] \quad (38)$$

where  $n_e$  and  $n_{lg}$  are the number of engines and landing gear mounted on the semispan, respectively;  $W_{e_i}$  and  $W_{lg_i}$  are the weights of the  $i^{th}$  engine and  $i^{th}$  landing gear, respectively;  $y_{e_i}$  and  $y_{lg_i}$  are the locations of the  $i^{th}$  engine and  $i^{th}$  landing gear, respectively; and

$$h_e(y_{e_i} - y) = \begin{cases} 1, & y_{e_i} > y \\ 0, & y_{e_i} < y \end{cases} \quad (39)$$

$$h_{lg}(y_{lg_i} - y) = \begin{cases} 1, & y_{lg_i} > y \\ 0, & y_{lg_i} < y \end{cases} \quad (40)$$

The bending moment is

$$M(y) = nK_S \left[ \frac{W}{S} A C_P - \frac{W_{FT}}{V_W} V C_g - \sum_{i=1}^{n_e} h_e(y_{e_i} - y) W_{e_i} (y_{e_i} - y) - \sum_{i=1}^{n_{lg}} h_{lg}(y_{lg_i} - y) W_{lg_i} (y_{lg_i} - y) \right] \quad (41)$$

### Structural Analysis

**Fuselage**– Weight estimating relationships are now developed for the load-carrying fuselage structure. In addition, the volume taken up by the fuselage structure is also determined.



Considering first the circular shell, the stress resultants in the axial direction caused by longitudinal bending, axial acceleration, and pressure at a fuselage station  $x$  are

$$N_{xB} = \frac{Mr}{I'_y} \quad (42)$$

$$N_{xA} = \frac{N_x W_S}{P} \quad (43)$$

$$N_{xP} = \frac{AP_g}{P} \quad (44)$$

respectively, where  $r = D/2$  is the fuselage radius,  $A = \pi r^2$  is the fuselage cross-sectional area, and  $P = 2\pi r$  is the fuselage perimeter. In equation 42,  $I'_y = \pi r^3$  is the moment of inertia of the shell divided by the shell thickness. In equation 43, for the case of fuselage-mounted propulsion,  $W_S$  is the portion of vehicle weight ahead of station  $x$  if  $x$  is ahead of the inlet entrance, or the portion of vehicle weight behind  $x$  if  $x$  is behind the nozzle exit. In equation 44,  $P_g$  is the limit gage pressure differential for the passenger compartment during cruise. The total tension stress resultant is then

$$N_x^+ = N_{xB} + N_{xP} \quad (45)$$

if  $x$  is ahead of the nozzle exit, and

$$N_x^+ = N_{xB} + N_{xP} + N_{xA} \quad (46)$$

if  $x$  is behind it. Similarly, the total compressive stress resultant is

$$N_x^- = N_{xB} + N_{xA} - \begin{cases} 0, & \text{if not pressure stabilized} \\ N_{xP}, & \text{if stabilized} \end{cases} \quad (47)$$

if  $x$  is ahead of the inlet entrance, and

$$N_x^- = N_{xB} - \begin{cases} 0, & \text{if not pressure stabilized} \\ N_{xP}, & \text{if stabilized} \end{cases} \quad (48)$$

if  $x$  is behind it. These relations are based on the premise that acceleration loads never decrease stress resultants, but pressure loads may relieve stress, if pressure stabilization is chosen as an option. The stress resultant in the hoop direction is

$$N_y = rP_g K_P \quad (49)$$

where  $K_P$  accounts for the fact that not all of the shell material (for example, the core material in sandwich designs) is available for resisting hoop stress.

The equivalent isotropic thicknesses of the shell are given by

$$\bar{t}_{SC} = \frac{N_x^-}{F_{cy}} \quad (50)$$

$$\bar{t}_{ST} = \frac{1}{F_{tu}} \max(N_x^+, N_y) \quad (51)$$

$$\bar{t}_{SG} = K_{mg} t_{mg} \quad (52)$$

for designs limited by compressive yield strength ( $F_{cy}$ ), ultimate tensile strength ( $F_{tu}$ ), and minimum gage, respectively. In equation 52,  $t_{mg}$  is a specified minimum material thickness and  $K_{mg}$  is a parameter relating  $\bar{t}_{SG}$  to  $t_{mg}$  which depends on the shell geometry.

A fourth thickness that must be considered is that for buckling critical designs,  $\bar{t}_{SB}$ , which will now be developed. The nominal vehicles of this study have integrally stiffened shells stabilized by ring frames. In the buckling analysis of these structures, the shell is analyzed as a wide column and the frames are sized by the Shanley criteria (ref. 6). Expressions are derived for the equivalent isotropic thickness of the shell required to preclude buckling,  $\bar{t}_{SB}$ , and for the *smear*ed equivalent isotropic thickness of the ring frames required to preclude general instability,  $\bar{t}_F$ . The analysis will be restricted to the case of cylindrical shells. The major assumptions are that the structural shell behaves as an Euler beam and that all structural materials behave elastically.

For the stiffened shell with frames concept, the common procedure of assuming the shell to be a wide column is adopted. If the frame spacing is defined as  $d$  and Young's modulus of the shell material is defined as  $E$ , the buckling equation is then

$$\frac{N_x^-}{dE} = \epsilon \left( \frac{\bar{t}_{SB}}{d} \right)^2 \quad (53)$$

or, solving for  $\bar{t}_{SB}$

$$\bar{t}_{SB} = \sqrt{\frac{N_x^- d}{E\epsilon}} \quad (54)$$

Fuselage structural geometry concepts are presented in table 1; values of the shell efficiency  $\epsilon$  for the various structural concepts are given in table 2. The structural shell geometries available are simply stiffened, Z-stiffened, and truss-core sandwich. We next size the frames to prevent general instability failure. The Shanley criterion is based on the premise that the frames act as elastic supports for the wide column; this criterion gives the smear<sup>ed</sup> equivalent thickness of the frames as

Table 1. Fuselage structural geometry concepts

| KCON sets<br>concept number |   |
|-----------------------------|---|
| 2                           | Simply stiffened shell, frames, sized for minimum weight in buckling      |
| 3                           | Z-stiffened shell, frames, best buckling                                  |
| 4                           | Z-stiffened shell, frames, buckling-minimum gage compromise               |
| 5                           | Z-stiffened shell, frames, buckling-pressure compromise                   |
| 6                           | Truss-core sandwich, frames, bestis, no frames, best buckling             |
| 9                           | Truss-core sandwich, no frames, buckling-minimum gage-pressure compromise |

Table 2. Fuselage structural geometry parameters

| Structural concept<br>(KCON) | $m$   | $\epsilon$ | $K_{mg}$ | $K_p$ | $K_{th}$ |
|------------------------------|-------|------------|----------|-------|----------|
| 2                            | 2     | 0.656      | 2.463    | 2.463 | 0.0      |
| 3                            | 2     | 0.911      | 2.475    | 2.475 | 0.0      |
| 4                            | 2     | 0.760      | 2.039    | 1.835 | 0.0      |
| 5                            | 2     | 0.760      | 2.628    | 1.576 | 0.0      |
| 6                            | 2     | 0.605      | 4.310    | 3.965 | 0.459    |
| 8                            | 1.667 | 0.4423     | 4.820    | 3.132 | 0.405    |
| 9                            | 1.667 | 0.3615     | 3.413    | 3.413 | 0.320    |

$$\bar{t}_{FB} = 2r^2 \sqrt{\frac{\pi C_F N_x^-}{K_{F1} d^3 E_F}} \quad (55)$$

where  $C_F$  is Shanley's constant,  $K_{F1}$  is a frame geometry parameter, and  $E_F$  is Young's modulus for the frame material. (See ref. 3 for a discussion of the applicability of this criterion and for a detailed derivation of the equations presented here.) If the structure is buckling critical, the total thickness is

$$\bar{t} = \bar{t}_{SB} + \bar{t}_{FB} \quad (56)$$

Minimizing  $\bar{t}$  with respect to  $d$  results in

$$\bar{t} = \frac{4}{27^{1/4}} \left( \frac{\pi C_F}{K_{F1} \epsilon^3 E_F E^3} \right)^{1/8} \left( \frac{2r^2 \rho_F (N_x^-)^2}{\rho} \right)^{1/4} \quad (57)$$

$$\bar{t}_{SB} = \frac{3}{4} \bar{t} \quad (58)$$

$$\bar{t}_{FB} = \frac{1}{4} \bar{t} \quad (59)$$

$$d = \left( 6r^2 \frac{\rho_F}{\rho} \sqrt{\frac{\pi C_F \epsilon E}{K_{F1} E_F}} \right)^{1/2} \quad (60)$$

where  $\rho_F$  is the density of the frame material and  $\rho$  is the density of the shell material, so that the shell is three times as heavy as the frames.

Frameless sandwich shell concepts may also be used. For these concepts, it is assumed that the elliptical shell buckles at the load determined by the maximum compressive stress resultant  $N_x^-$  on the cylinder. The buckling equation for these frameless sandwich shell concepts is

$$\frac{N_x^-}{rE} = \epsilon \left( \frac{\bar{t}_{SB}}{r} \right)^m \quad (61)$$

where  $m$  is the buckling equation exponent. Or, solving for  $\bar{t}_{SB}$

$$\bar{t}_{S_B} = r \left( \frac{N_x^-}{rE\epsilon} \right)^{\frac{1}{m}} \quad (62)$$

This equation is based on small deflection theory, which seems reasonable for sandwich cylindrical shells, although it is known to be inaccurate for monocoque cylinders. Values of  $m$  and  $\epsilon$  may be found, for example in references 9 and 10 for many shell geometries. Table 2 gives values for sandwich structural concepts available in PDCYL, numbers 8 and 9, both of which are truss-core sandwich. The quantities  $N_x^-$ ,  $r$ , and consequently  $\bar{t}_{S_B}$ , will vary with fuselage station dimension  $x$ .

At each fuselage station  $x$ , the shell must satisfy all failure criteria and meet all geometric constraints. Thus, the shell thickness is selected according to compression, tension, minimum gage, and buckling criteria, or

$$\bar{t}_S = \max(\bar{t}_{S_C}, \bar{t}_{S_T}, \bar{t}_{S_G}, \bar{t}_{S_B}) \quad (63)$$

If  $\bar{t}_S = \bar{t}_{S_B}$ , the structure is buckling critical and the equivalent isotropic thickness of the frames,  $\bar{t}_F$ , is computed from equation 59. If  $\bar{t}_S > \bar{t}_{S_B}$ , the structure is not buckling critical at the optimum frame sizing and the frames are resized to make  $\bar{t}_S = \bar{t}_{S_B}$ . Specifically, a new frame spacing is computed from equation 54 as

$$d = \frac{E\epsilon\bar{t}_S^2}{N_x^-} \quad (64)$$

and this value is used in equation 55 to determine  $\bar{t}_F$ .

The total thickness of the fuselage structure is then given by the summation of the smeared weights of the shell and the frames

$$\bar{t}_B = \bar{t}_S + \bar{t}_F \quad (65)$$

The shell gage thickness may be computed from  $\bar{t}_g = \bar{t}_S / K_{mg}$ . The *ideal* fuselage structural weight is obtained by summation over the vehicle length

$$W_I = 2\pi \sum (\rho\bar{t}_{S_i} + \rho_F\bar{t}_{F_i})r_i\Delta x_i \quad (66)$$

where the quantities subscripted  $i$  depend on  $x$ .

We next discuss the derivation of the structural geometry parameters shown in table 2. The Z-stiffened shell, typical of modern transport aircraft, will be used as an example of skin-stringer-frame construction. Using reference 9 and figure 6, the equivalent isotropic thickness of the smeared skin and stringers is

$$\bar{t}_S = t_s + \frac{2b_f f_f}{b_s} + \frac{b_w t_w}{b_s} = \left[ 1 + 1.6 \left( \frac{b_w}{b_s} \right) \left( \frac{t_w}{t_s} \right) \right] t_s \quad (67)$$

Since only the skin is available for resisting pressure loads,

$$K_p = 1 + 1.6 \left( \frac{b_w}{b_s} \right) \left( \frac{t_w}{t_s} \right) \quad (68)$$

For minimum gage designs, if  $t_s > t_w$  then  $t_w = t_{mg}$  and

$$\bar{t}_S = \left[ \left( \frac{t_s}{t_w} \right) + 1.6 \left( \frac{b_w}{b_s} \right) \right] t_{mg} \quad (69)$$

so that

$$K_{mg} = \left( \frac{t_s}{t_w} \right) + 1.6 \left( \frac{b_w}{b_s} \right) \quad (70)$$

On the other hand, if  $t^s < t^w$  then  $t_s = t_{mg}$  and

$$\bar{t}_S = \left[ 1 + 1.6 \left( \frac{b_w}{b_s} \right) \left( \frac{t_w}{t_s} \right) \right] t_{mg} \quad (71)$$

so that

$$K_{mg} = 1 + 1.6 \left( \frac{b_w}{b_s} \right) \left( \frac{t_w}{t_s} \right) \quad (72)$$

Equations 68, 70, and 72 show that for both pressure loading critical and minimum gage limited structure,  $(b_w/b_s)$  and  $(t_w/t_s)$  should be as small as possible (i.e., no stringers). As an option in PDCYL, all of the detailed shell dimensions shown in figure 6 are computed and output at each fuselage station.

In practice, a typical design will be influenced by bending and pressure loads and by the minimum gage constraint, and thus a compromise is necessary. If buckling is of paramount importance, then a good choice is  $(b_w/b_s) = 0.87$  and  $(t_w/t_s) = 1.06$  because this gives the maximum buckling efficiency for this concept, namely  $\epsilon = 0.911$  (ref. 9). From equations 68 and 72,

$$K_p = K_{mg} = 1 + (1.6)(0.87)(1.06) = 2.475 \quad (73)$$

This is concept 3 in tables 1 and 2. If pressure dominates the loading condition, then  $(b_w/b_s) = 0.6$  and  $(t_w/t_s) = 0.6$  is a reasonable choice, giving  $\epsilon = 0.76$ ,  $K_p = 1.576$ , and  $K_{mg} = 2.628$ ; this is concept 5. For minimum gage dominated structure, the geometry  $(b_w/b_s) = 0.58$  and  $(t_w/t_s) = 0.90$  gives concept 6.

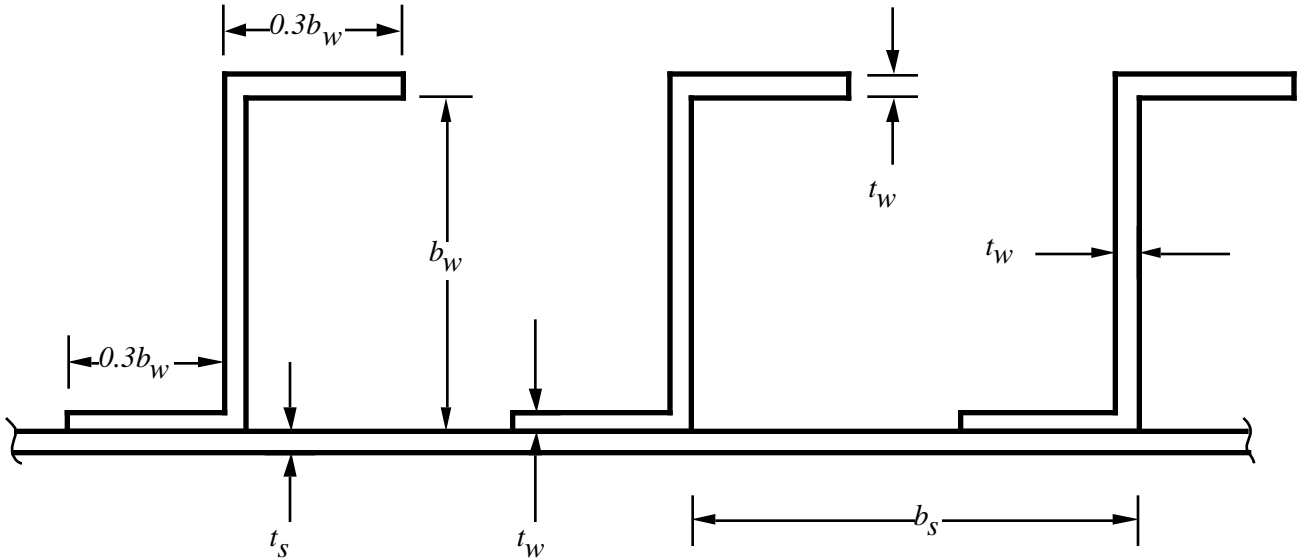


Figure 6. Typical Z-stiffened shell geometry.

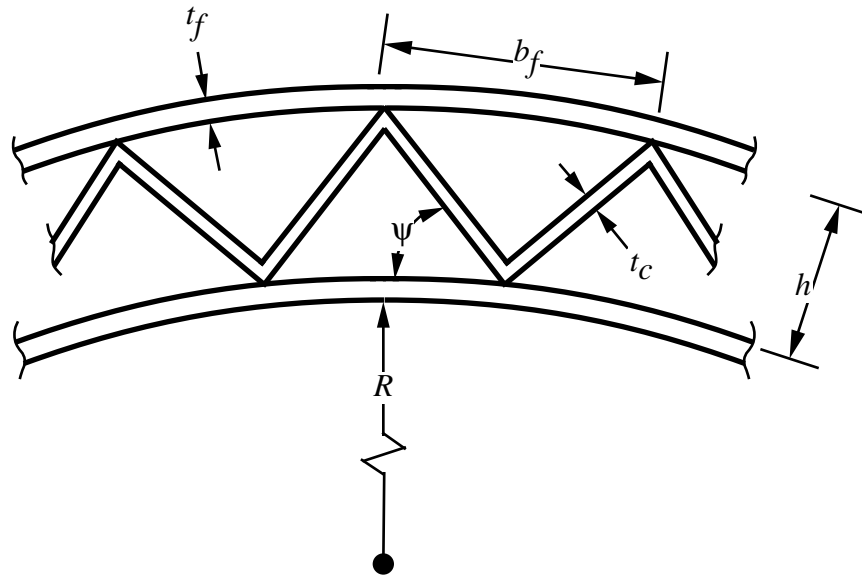


Figure 7. Truss-core sandwich geometry.

The geometry of the truss-core sandwich shell concept is shown in figure 7. The equivalent isotropic shell thickness of this concept is

$$\bar{t}_S = \left( 2 + \frac{t_c}{t_f} \frac{1}{\cos(\psi)} \right) t_f \quad (74)$$

Reference 9 shows that the optimum buckling efficiency is obtained for  $(t_c/t_f) = 0.65$  and  $\psi = 55$  deg. This gives

$\varepsilon = 0.4423$ ,  $K_{mg} = 4.820$ , and  $K_p = 3.132$ , concept 8 in tables 1 and 2. To get a design that is lighter for minimum gage dominant structure, a geometry is chosen that places equal thickness material in the face sheets and the core; the choice of  $(t_c/t_f) = 1.0$  and  $\psi = 45$  deg gives structural concept 9. These calculations assume that the face sheets and core are composed of the same material and are subject to the same minimum gage constraint.

Since the preceding analysis gives only the ideal weight,  $W_I$ , the *nonoptimum* weight,  $W_{NO}$  (including fasteners, cutouts, surface attachments, uniform gage penalties, manufacturing constraints, etc.) has yet to be determined. The method used will be explained in a later section.

**Wing**– Using the geometry and loads applied to the wing developed above, the structural dimensions and weight of the structural box may now be calculated. The wing structure is assumed to be a rectangular multi-web box beam with the webs running in the direction of the structural semispan. Reference 9 indicates that the critical instability mode for multi-web box beams is simultaneous buckling of the covers due to local instability and of the webs due to flexure induced crushing. This reference gives the solidity (ratio of volume of structural material to total wing box volume) of the least weight multi-web box beams as

$$\Sigma = \varepsilon \left( \frac{M}{Z_S t^2 E} \right)^e \quad (75)$$

where  $\varepsilon$  and  $e$  depend on the cover and web geometries (table 3),  $M$  is the applied moment,  $t$  is the thickness,  $E$  is the elastic modulus, and  $Z_S$  is obtained from reference 9. The solidity is therefore

$$\Sigma = \frac{W'_{BEND}(y)}{\rho Z_S t} \quad (76)$$

where  $W'_{BEND}$  is the weight of bending material per unit span and  $\rho$  is the material density.  $W'_{BEND}$  is computed from equations 75 and 76. The weight per unit span of the shear material is

$$W'_{SHEAR}(y) = \frac{\rho F_S}{\sigma_S} \quad (77)$$

where  $F_S$  is the applied shear load and  $\sigma_S$  is the allowable shear stress. The optimum web spacing (fig. 8) is computed from (ref. 2)

$$d_W = t \left[ \frac{(1-2e_C)}{(1-e_C)\sqrt{2\varepsilon_W}} \left( \frac{M}{Z_S t^2 E} \right)^{\frac{2e_C-3}{2e_C}} \varepsilon_C \frac{3}{2e_C} \right]^{\frac{2e_C}{4e_C-3}} \quad (78)$$

where subscripts  $W$  and  $C$  refer to webs and covers, respectively. The equivalent isotropic thicknesses of the covers and webs are

$$\bar{t}_C - d_W \left( \frac{M}{Z_S t E \varepsilon_C d_W} \right)^{\frac{1}{e_C}} \quad (79)$$

$$\bar{t}_W = t \sqrt[3]{ \left( \frac{M}{Z_S t^2 E} \right)^{\left( 2 - \frac{1}{e_C} \right)} \left( \frac{\varepsilon_C d_W}{t} \right)^{\frac{1}{e_C}} \left( \frac{2}{\varepsilon_W} \right) } \quad (80)$$

respectively, and the gage thicknesses are

$$t_{gC} = K_{gC} \bar{t}_C \quad (81)$$

$$t_{gW} = K_{gW} \bar{t}_W \quad (82)$$

Values of  $\varepsilon$ ,  $e$ ,  $\varepsilon_C$ ,  $E_C$ ,  $\varepsilon_W$ ,  $K_{gW}$ , and  $K_{gC}$  are found in table 3 for various structural concepts (ref. 9). If the wing structural semispan is divided into  $N$  equal length segments, the total *ideal* weight of the wing box structure is

$$W_{BOX} = \frac{2b_S}{N} \sum_{i=1}^N \left( W'_{BEND_i} + W'_{SHEAR_i} \right) \quad (83)$$

Table 3. Wing structural coefficients and exponents

| Covers      | Webs        | $\varepsilon$ | $e$   | $\varepsilon$ | $e_C$ | $\varepsilon_W$ | $K_{gC}$ | $K_{gW}$ |
|-------------|-------------|---------------|-------|---------------|-------|-----------------|----------|----------|
| Unstiffened | Truss       | 2.25          | 0.556 | 3.62          | 3     | 0.605           | 1.000    | 0.407    |
| Unstiffened | Unflanged   | 2.21          | 0.556 | 3.62          | 3     | 0.656           | 1.000    | 0.505    |
| Unstiffened | Z-stiffened | 2.05          | 0.556 | 3.62          | 3     | 0.911           | 1.000    | 0.405    |
| Truss       | Truss       | 2.44          | 0.600 | 1.108         | 2     | 0.605           | 0.546    | 0.407    |
| Truss       | Unflanged   | 2.40          | 0.600 | 1.108         | 2     | 0.656           | 0.546    | 0.505    |
| Truss       | Z-stiffened | 2.25          | 0.600 | 1.108         | 2     | 0.911           | 0.546    | 0.405    |

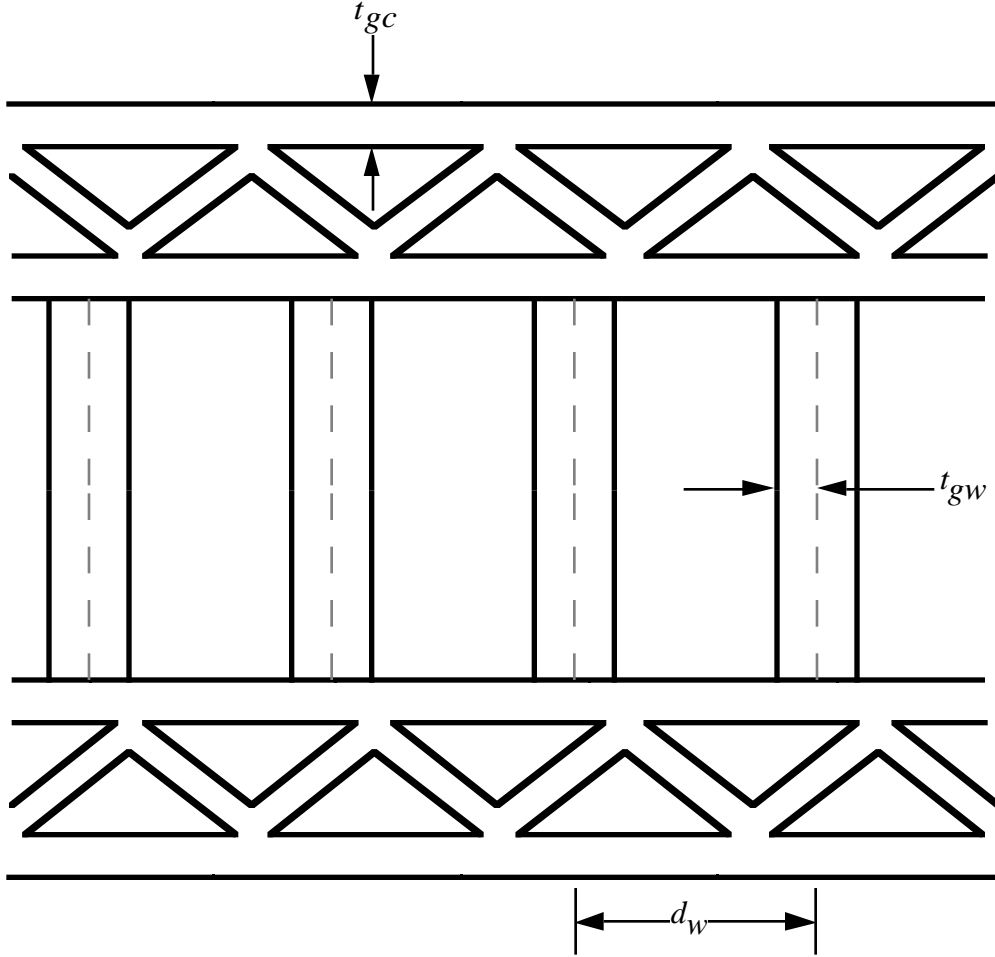


Figure 8. Wing structural concept.

The wing carrythrough structure consists of torsion material in addition to bending and shear material. The torsion material is required to resist the twist induced due to the sweep of the wing. The bending material is computed in a similar manner as that of the box except that only the longitudinal component of the bending moment contributes. Letting  $t_0 = t(y = 0)$  and  $M_0 = M(y = 0)$ ,

$$\Sigma_C = \varepsilon \left( \frac{M_0 \cos(\Lambda_S)}{t_0^2 C_{SR} E} \right)^e \quad (84)$$

The weight of the bending material is then

$$W_{BEND_C} = \rho \Sigma_C C_{SR} t_0 w_C \quad (85)$$

where  $w_C$  is the width of the carrythrough structure. (When the wing-fuselage intersection occurs entirely within the cylindrical midsection, as is the case with all eight transport used for validation in the present study,  $w_C = D$ .) The quantities  $d_w$ ,  $t_w$ , and  $t_C$  are computed in

the same manner as for the box. The weight of the shear material is

$$W_{SHEAR_C} = \rho \frac{F_{S_0}}{\sigma_S} w_C \quad (86)$$

where  $F_{S_0} = F_S(0)$ .

The torque on the carrythrough structure is

$$T = M_0 \sin(\Lambda_S) \quad (87)$$

and the weight of the torsion material is then

$$W_{TORSION_C} = \frac{\rho T (t_0 + C_{SR}) w_C}{t_0 C_{SR} \sigma_S} \quad (88)$$

Finally, the *ideal* weight of the carrythrough structure is computed from a summation of the bending shear and torsion material, or

$$W_C = W_{BEND_C} + W_{SHEAR_C} + W_{TORSION_C} \quad (89)$$

As in the case of the fuselage structural weight, *nonoptimum* weight must be added to the ideal weight to obtain the true wing structural weight. The method used will be discussed below.

The static deflection of the wingtip under the pull-up maneuver is also determined. Using the moment-area method applied to an Euler beam (ref. 11), the deviation of point *B* on the deflected surface from the tangent drawn from another point *A* on the surface is equal to the area under the  $M/(EI)$  diagram between *A* and *B* multiplied by the distance to the centroid of this area from *B*,

$$t_{BA} = \int_B^A y d\theta = \int_B^A \frac{M}{EI} y dy \quad (90)$$

where  $\theta$  is the angular displacement of the beam and  $y$  is the longitudinal axis of the beam. For the case of a wing with trapezoidal planform, the longitudinal axis,  $y$ , will lie along the quarter-chord line (fig. 3). For a wing with a horizontal unloaded configuration, the tangential deviation,  $t_{BA}$ , will equal the true vertical tip displacement (assumed to be the case). Only the wing cover contributes to the bending resistance, while the webs offer similar shear stiffness. The wing area moment of inertia,  $I$ , at any structural semispan station  $y$  is determined with the Parallel Axis theorem, as cover thickness is small when compared with total wing thickness.

## Regression Analysis

**Overview**— Using fuselage and wing weight statements of eight subsonic transports, a relation between the calculated load-bearing structure weights obtained through PDCYL and the actual load-bearing structure weights, primary structure weights, and total weights is determined using statistical analysis techniques. A basic application which is first described is linear regression, wherein the estimated weights of the aircraft are related to the weights calculated by PDCYL with a straight line,  $y = mx + b$ , where  $y$  is the value of the estimated weight,  $m$  is the slope of the line,  $x$  is the value obtained through PDCYL, and  $b$  is the  $y$ -intercept. This line is termed a *regression* line, and is found by using the *method of least squares*, in which the sum of the squares of the residual errors between actual data points and the corresponding points on the regression line is minimized. Effectively, a straight line is drawn through a set of ordered pairs of data (in this case eight weights obtained through PDCYL and the corresponding actual weights) so that the aggregate deviation of the actual weights above or below this line is minimized. The estimated weight is therefore dependent upon the independent PDCYL weight.

As an example, if the form of the regression equation is linear, the estimated weight is

$$y_{est} = mx_{calc} + b \quad (91)$$

where  $m$  is the slope,  $b$  is the intercept, and  $x_{calc}$  is the weight PDCYL calculates. The resulting residual to be minimized is

$$E = \sum_{i=1}^n (y_{actual_i} - y_{est_i})^2 \quad (92)$$

or

$$E = \sum_{i=1}^n (y_{actual_i} - mx_{calc_i} - b)^2 \quad (93)$$

where  $y_{actual}$  is the actual component weight and  $n$  is the number of aircraft whose data are to be used in the fit. By taking partial derivatives of the residual error with respect to both  $m$  and  $b$ , equations for the values of these two unknown variables are found to be

$$m = \frac{n \sum_{i=1}^n x_{calc_i} y_{act_i} - \sum_{i=1}^n x_{calc_i} \sum_{i=1}^n y_{act_i}}{n \sum_{i=1}^n x_{calc_i}^2 - \left( \sum_{i=1}^n x_{calc_i} \right)^2} \quad (94)$$

$$b = \bar{y}_{act} - n\bar{x}_{calc} \quad \bar{x}, \bar{y} = \text{mean values of } x \text{ and } y \quad (95)$$

Of key importance is the degree of accuracy to which the prediction techniques are able to estimate actual aircraft weight. A measure of this accuracy, the correlation coefficient, denoted  $R$ , represents the reduction in residual error due to the regression technique.  $R$  is defined as

$$R = \sqrt{\frac{E_t - E_r}{E_r}} \quad (96)$$

where  $E_t$  and  $E_r$  refer to the residual errors associated with the regression before and after analysis is performed, respectively. A value of  $R = 1$  denotes a perfect fit of the data with the regression line. Conversely, a value of  $R = 0$  denotes no improvement in the data fit due to regression analysis.

There are two basic forms of equations which are implemented in this study. The first is of the form

$$y_{est} = mx_{calc} \quad (97)$$

The second general form is

$$y_{est} = mx_{calc}^a \quad (98)$$

The first form is a simplified version of the linear example as discussed above, with the  $y$ -intercept term set to zero. However, because the second general equation is not linear, nor can it be transformed to a linear equation, an alternative method must be employed. In order to formulate the resulting *power-intercept* regression equation, an iterative approach developed by D. W. Marquardt is utilized (ref. 12). This algorithm starts at a certain point in space, and, by applying the method of steepest descent, a gradient is obtained which indicates the direction in which the most rapid decrease in the residual errors will occur. In addition, the Taylor Series method produces a second similar vector. Interpolation between these two vectors yields a direction in which to move the point in order to minimize the associated error. After several iterations, the process converges to a minimum value. It should be noted that there may be several local minimums and there is no guarantee that the method converges to the global one.

**Fuselage**– The analysis above is used to develop a relationship between weight calculated by PDCYL and actual wing and fuselage weights. The data were obtained from detailed weight breakdowns of eight transport aircraft (refs. 13–17) and are shown in table 4 for the fuselage. Because the theory used in the PDCYL analysis only predicts the load-carrying structure of the aircraft components, a correlation between the predicted weight and the actual load-carrying structural weight and primary weight, as well as the total weight of the fuselage, was made.

Structural weight consists of all load-carrying members including bulkheads and frames, minor frames, covering, covering stiffeners, and longerons. For the linear curve-fit, the resulting regression equation is

$$W_{actual} = 1.3503W_{calc} \quad R = 0.9946 \quad (99)$$

This shows that the *nonoptimum* factor for fuselage structure is 1.3503; in other words, the calculated weight must be increased by about 35 percent to get the actual structural weight. For the alternative power-intercept curve fitting analysis, the resulting load-carrying regression equation is

$$W_{actual} = 1.1304W_{calc}^{1.0179} \quad R = 0.9946 \quad (100)$$

To use either of these equations to estimate total fuselage weight, nonstructural weight items must be estimated independently and added to the structural weight.

Primary weight consists of all load-carrying members as well as any secondary structural items such as joints fasteners, keel beam, fail-safe straps, flooring, flooring structural supplies, and pressure web. It also includes the lavatory structure, galley support, partitions, shear ties, tie rods, structural firewall, torque boxes, and attachment fittings. The linear curve fit for this weight yields the following primary regression equation

$$W_{actual} = 1.8872W_{calc} \quad R = 0.9917 \quad (101)$$

The primary power-intercept regression equation is

$$W_{actual} = 1.6399W_{calc}^{1.0141} \quad R = 0.9917 \quad (102)$$

Table 4. Fuselage weight breakdowns for eight transport aircraft

| Aircraft | Weight, lb |                         |                   |                 |
|----------|------------|-------------------------|-------------------|-----------------|
|          | PDCYL      | Load-carrying structure | Primary structure | Total structure |
| B-720    | 6545       | 9013                    | 13336             | 19383           |
| B-727    | 5888       | 8790                    | 12424             | 17586           |
| B-737    | 3428       | 5089                    | 7435              | 11831           |
| B-747    | 28039      | 39936                   | 55207             | 72659           |
| DC-8     | 9527       | 13312                   | 18584             | 24886           |
| MD-11    | 20915      | 25970                   | 34999             | 54936           |
| MD-83    | 7443       | 9410                    | 11880             | 16432           |
| L-1011   | 21608      | 28352                   | 41804             | 52329           |



The total fuselage weight accounts for all members of the body, including the structural weight and primary weight. It does not include passenger accommodations, such as seats, lavatories, kitchens, stowage, and lighting; the electrical system; flight and navigation systems; lighting gear; fuel and propulsion systems; hydraulic and pneumatic systems; the communication system; cargo accommodations; flight deck accommodations; air conditioning equipment; the auxiliary power system; and emergency systems. Linear regression results in the following total fuselage weight equation

$$W_{actual} = 2.5686W_{calc} \quad R = 0.9944 \quad (103)$$

This shows that the nonoptimum factor for the total fuselage weight is 2.5686; in other words, the fuselage

structure weight estimated by PDCYL must be increased by about 157 percent to get the actual total fuselage weight. This nonoptimum factor is used to compare fuselage structure weight estimates from PDCYL with total fuselage weight estimates from the Sanders and the Air Force equations used by ACSYNT.

The total fuselage weight power-intercept regression equation is

$$W_{actual} = 3.9089W_{calc}^{0.9578} \quad R = 0.9949 \quad (104)$$

Plots of actual fuselage component weight versus PDCYL-calculated weight, as well as the corresponding linear regressions, are shown in figures 9–11.

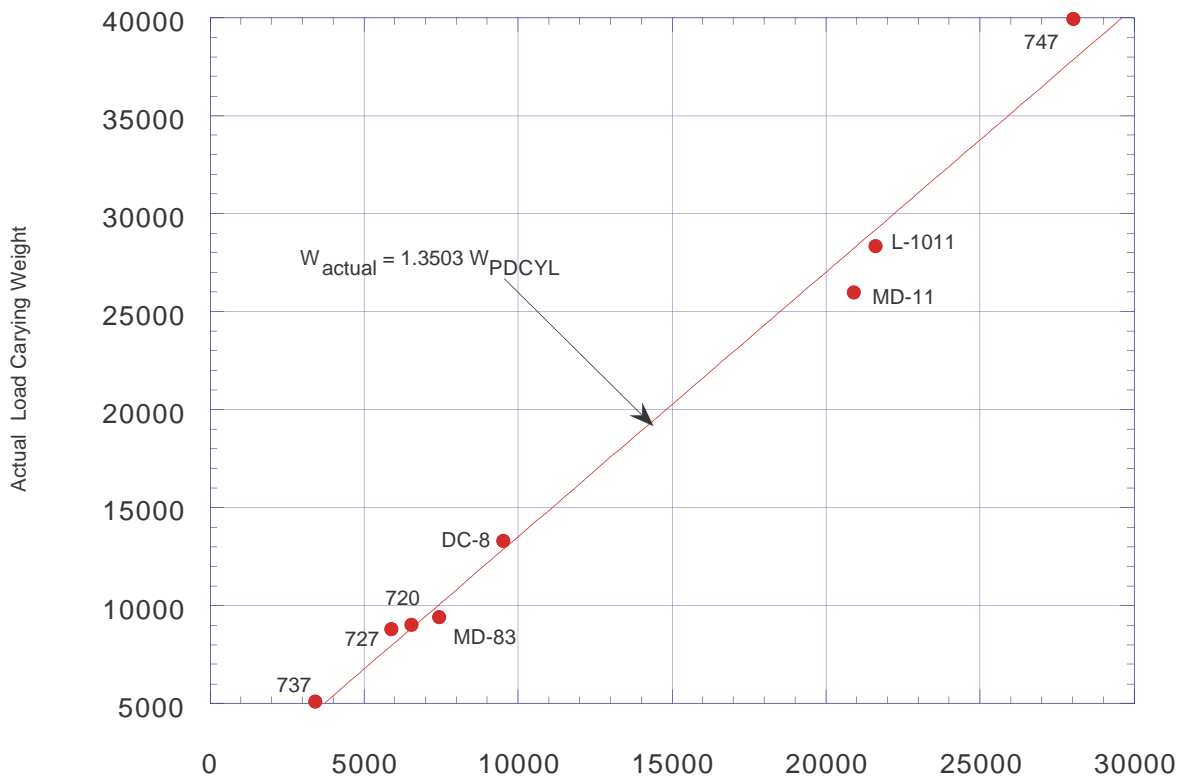


Figure 9. Fuselage load-carrying structure and linear regression.

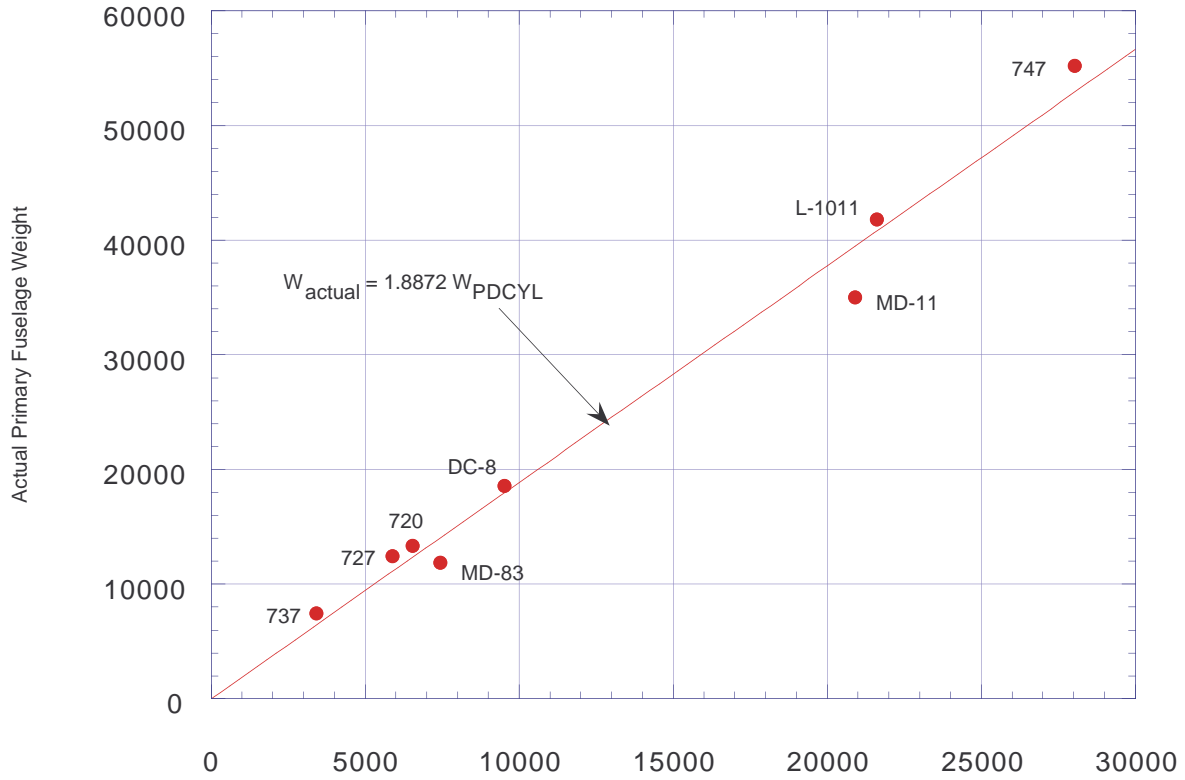


Figure 10. Fuselage primary structure and linear regression.

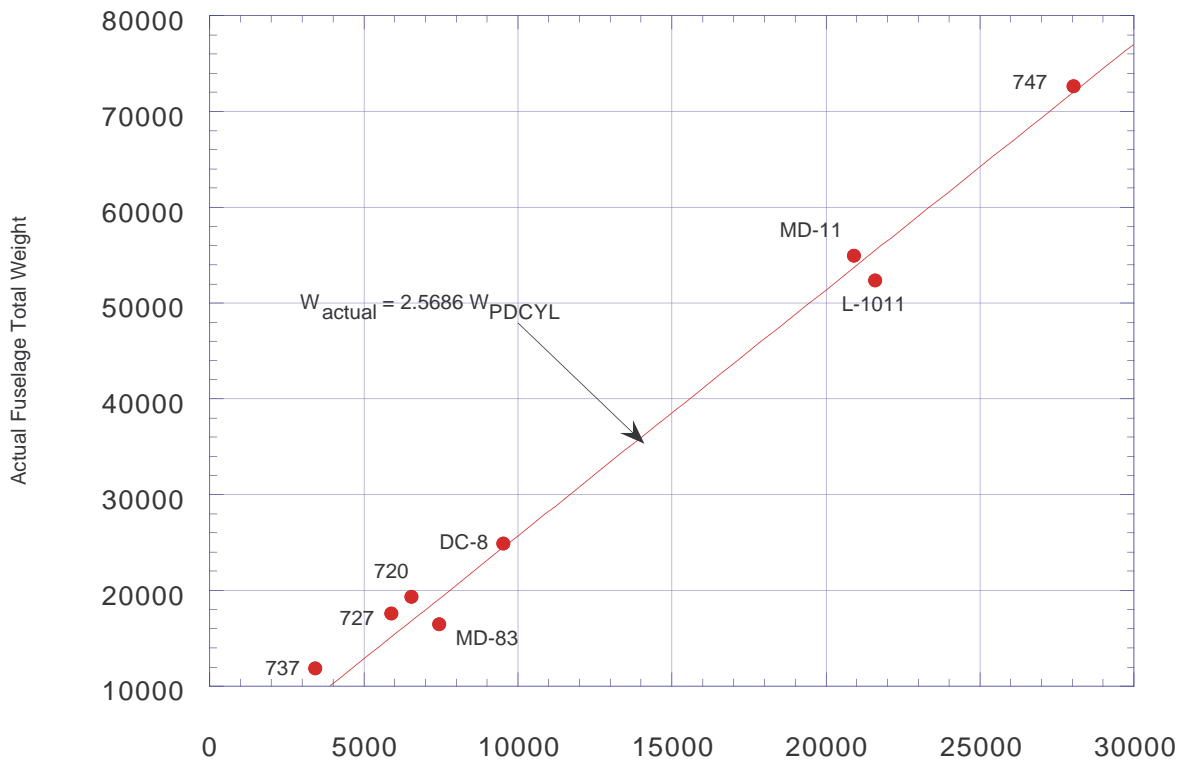


Figure 11. Fuselage total structure and linear regression.

Table 5. Wing weight breakdowns for eight transport aircraft

| Aircraft | Weight, lb |                         |                   |                 |
|----------|------------|-------------------------|-------------------|-----------------|
|          | PDCYL      | Load-carrying structure | Primary structure | Total structure |
| B-720    | 13962      | 11747                   | 18914             | 23528           |
| B-727    | 8688       | 8791                    | 12388             | 17860           |
| B-737    | 5717       | 5414                    | 7671              | 10687           |
| B-747    | 52950      | 50395                   | 68761             | 88202           |
| DC-8     | 22080      | 19130                   | 27924             | 35330           |
| MD-11    | 33617      | 35157                   | 47614             | 62985           |
| MD-83    | 6953       | 8720                    | 11553             | 15839           |
| L-1011   | 25034      | 28355                   | 36101             | 46233           |

**Wing**– The same analysis was performed on the wing weight for the sample aircraft and is shown in table 5. The wing box, or load-carrying structure, consists of spar caps, interspar coverings, spanwise stiffeners, spar webs, spar stiffeners, and interspar ribs. The wing box linear regression equation is

$$W_{actual} = 0.9843W_{calc} \quad R = 0.9898 \quad (105)$$

so that the nonoptimum factor is 0.9843. Power-intercept regression results in

$$W_{actual} = 1.3342W_{calc}^{0.9701} \quad R = 0.9902 \quad (106)$$

Wing primary structural weight includes all wing box items in addition to auxiliary spar caps and spar webs, joints and fasteners, landing gear support beam, leading and trailing edges, tips, structural firewall, bulkheads, jacket fittings, terminal fittings, and attachments. Linear regression results in

$$W_{actual} = 1.3442W_{calc} \quad R = 0.9958 \quad (107)$$

Power-intercept regression yields

$$W_{actual} = 2.1926W_{calc}^{0.9534} \quad R = 0.9969 \quad (108)$$

The total wing weight includes wing box and primary weight items in addition to high-lift devices, control surfaces, and access items. It does not include the propulsion system, fuel system, and thrust reversers; the electrical system; alighting gear; hydraulic and pneumatic systems; anti-icing devices; and emergency systems. The resulting total weight linear regression equation is

$$W_{actual} = 1.7372W_{calc} \quad R = 0.9925 \quad (109)$$

This shows that the nonoptimum factor for the total wing weight is 1.7372; in other words, the wing box weight estimated by PDCYL must be increased by about 74 percent to get the actual total wing weight. This nonoptimum factor is used to compare wing box weight estimates from PDCYL with total wing weight estimates from the Sanders and the Air Force equations used by ACSYNT.

The power-intercept equation for total wing weight is

$$W_{actual} = 3.7464W_{calc}^{0.9268} \quad R = 0.9946 \quad (110)$$

Plots of actual wing component weight versus PDCYL-calculated weight, as well as the corresponding linear regressions, are shown in figures 12–14.

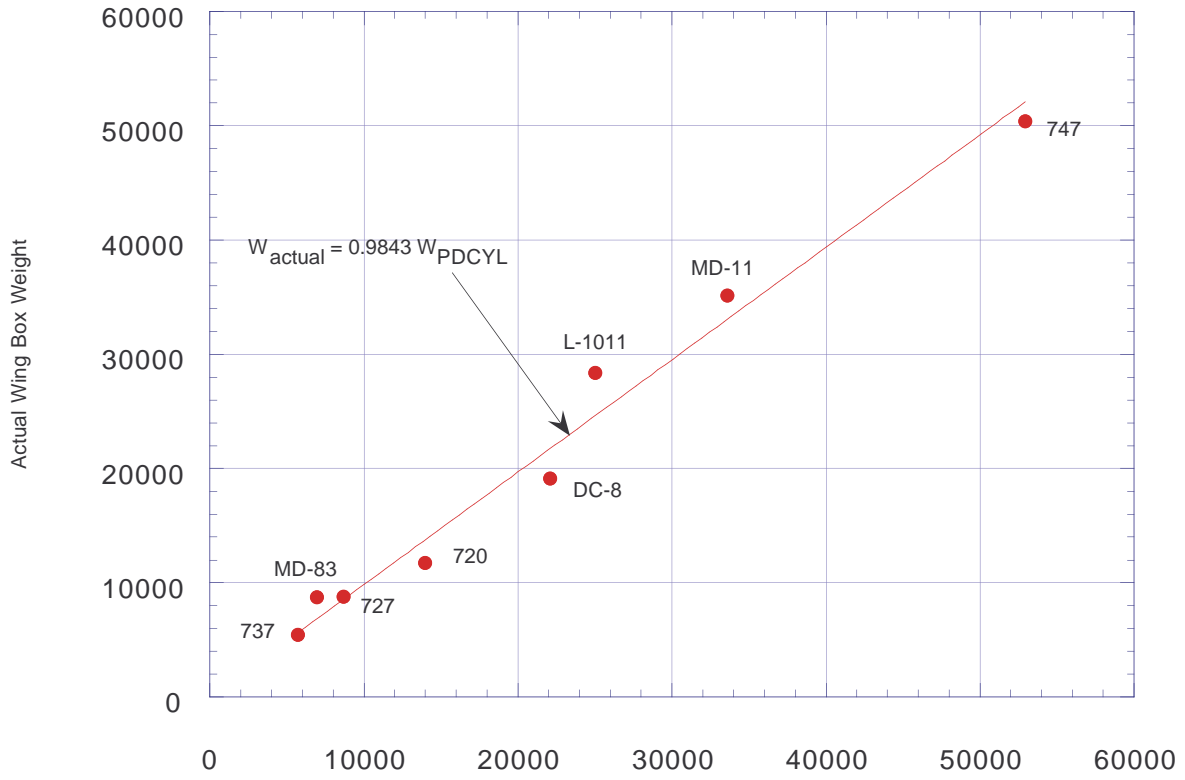


Figure 12. Wing load-carrying structure and linear regression.

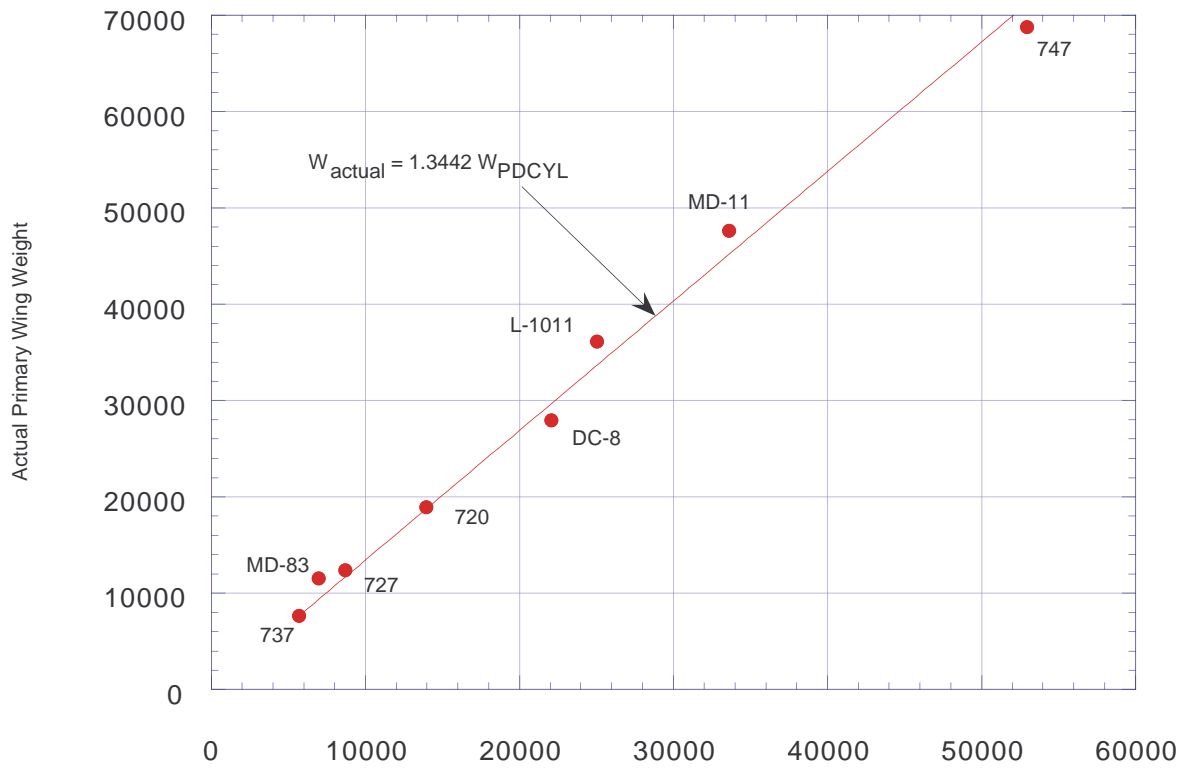


Figure 13. Wing primary structure and linear regression.

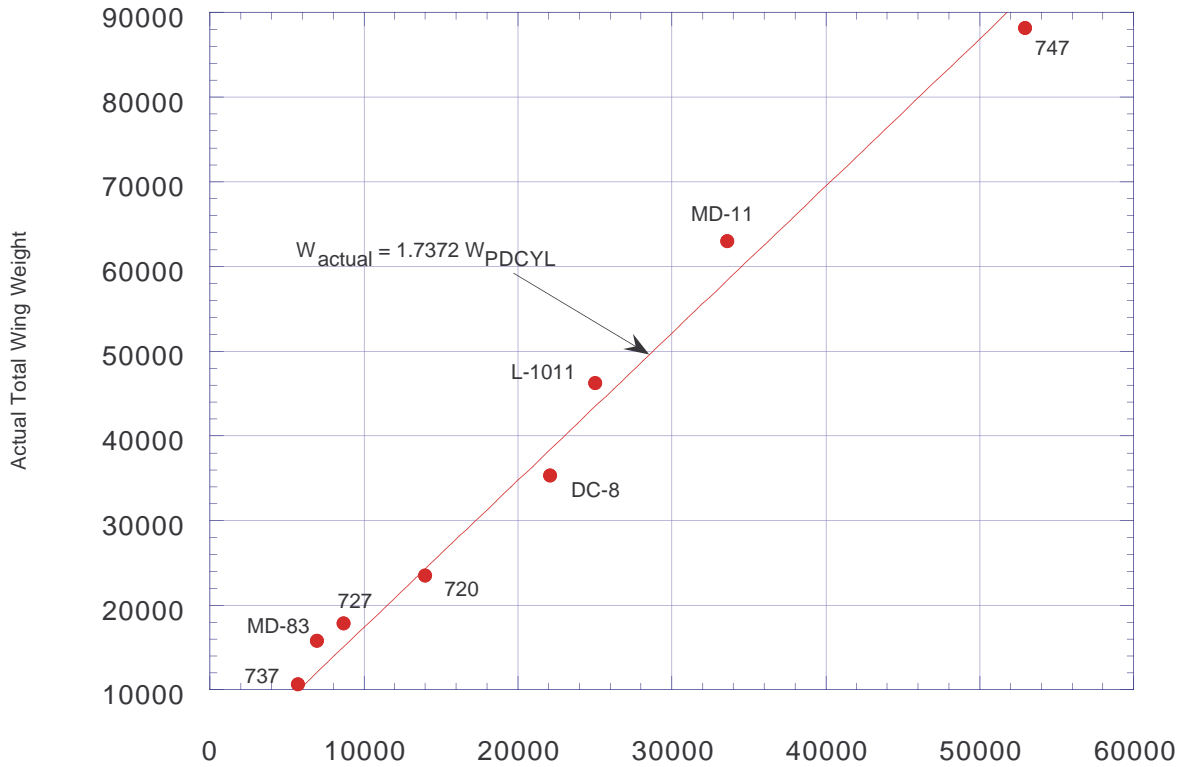


Figure 14. Wing total structure and linear regression.

**Discussion**– Both fuselage and wing weight linear and power regressions give excellent correlation with the respective weights of existing aircraft, as evidenced by the high values of the correlation coefficient,  $R$ . It should be noted that even though the power-based regressions give correlations equal to or better than the linear regressions their factors may vary distinctly from the linear cases. This is due to their powers not equaling unity.

Because estimates of non-load-bearing primary structure are generally not available at the conceptual design stage, and because nonprimary structure is probably not well estimated by a nonoptimum factor, equations 101 and 107 are recommended for estimating the primary structural weights of the respective transport fuselage and wing structures (figs. 10 and 13).

## Appendix A – User’s Manual, Example

### Description

The purpose of this appendix is to give a detailed example of the input procedure used to allow PDCYL to calculate fuselage and wing weights for a sample transport aircraft during an ACSYNT run. A sample output from PDCYL will also be given. The Boeing 747-21P will be used for the example. The layout of the 747-21P is shown in figure 15. The weights of the load-carrying portions of the fuselage and wing box for the 747-21P will be calculated by PDCYL and scaled by the respective nonoptimum factors developed earlier to give estimates for the weights of the fuselage and wing. A comparison between methods currently used by ACSYNT to estimate fuselage and wing weights and PDCYL output will be made with the corresponding actual weights of the 747-21P.

### Input

PDCYL requires input from both the existing ACSYNT data structure and an additional namelist containing data required by PDCYL which are not contained within the current ACSYNT format. There are three steps to run PDCYL within ACSYNT. First, the aircraft type is specified in the ACSYNT Control input. Currently the Transport Aircraft type is used. Second, data within ACSYNT module namelists are required. The ACSYNT Geometry, Trajectory, and Weights modules supply data for PDCYL execution. PDCYL uses the WING, HTAIL, VTAIL, FUS, WPOD, and FPOD namelists from the Geometry module. From the Trajectory module, the TRDATA namelist is used. From the Weights module the OPTS namelist is used. Third, data from the PDCYLIN namelist are used.

Variables used from ACSYNT namelists and the PDCYLIN namelist are given in tables 6 and 7, respectively. Default values for all variables are also given. These default values match the Boeing 747-21P. Key configuration parameters are given for each of the eight aircraft used in the validation study in table 8. An example of the PDCYLIN namelist input for the 747-21P is shown in figure 16.

A description of the specific structural concepts used to model both the fuselage and wing is given in the Structural Analysis section. As was noted earlier, the typical modern transport aircraft fuselage is a Z-stiffened shell. The buckling-minimum material gage compromise was

employed because it gives the lowest-weight (optimal) structure for the eight aircraft investigated in this study.

### Output

PDCYL weights output begins with the wing box and carrythrough structure analysis. The wing is sized during a quasi-static pull-up maneuver where the load factor is set equal to the ultimate load factor (nominally 3.75). Wing output contains three parts. First is the overall geometrical configuration. Second is a detailed station-by-station bending, shear, and torsion analysis and corresponding geometrical sizing along the span. Third is the detailed geometrical layout, loading, and weight breakdown of the carrythrough structure, weight breakdown of the wing components, and deflection of the wingtip. This wing weight is multiplied by the nonoptimum factor and returned to ACSYNT. An example of the PDCYL wing weight output for the 747-21P is shown in figure 17.

Next, the fuselage is analyzed. Fuselage output contains four parts. First is the overall geometrical layout and weight breakdown. Second is a station-by-station bending, shear, and axial stress analysis. Up to three load cases are investigated. In order they are a quasi-static pull-up maneuver, a landing maneuver, and travel over runway bumps. Third, the envelope of worst-case loading is shown for each station, from which the shell and frames are sized. Corresponding unit weight breakdowns are also given. As an option, the detailed geometric configuration at each station may be output. Fourth, weights summaries are given for the top and bottom sections of the fuselage (nominally the same). These summaries are then averaged to give the weight summary of the entire fuselage. The fuselage weight, including the corresponding nonoptimum factor, is returned to ACSYNT. An example of the PDCYL fuselage weight output for the 747-21P is shown in figure 18.

Figure 19(a) shows a comparison between fuselage weight estimates from the Sanders equation, the Air Force equation, and PDCYL with the actual fuselage weight of the 747-21P. Figure 19(b) shows a similar comparison for the wing weight. SLOPE and TECH factors were set to one for the comparisons in Figures 19(a) and 19(b), while the nonoptimum factors are those relating PDCYL estimations of structure weight to respective total component weight.

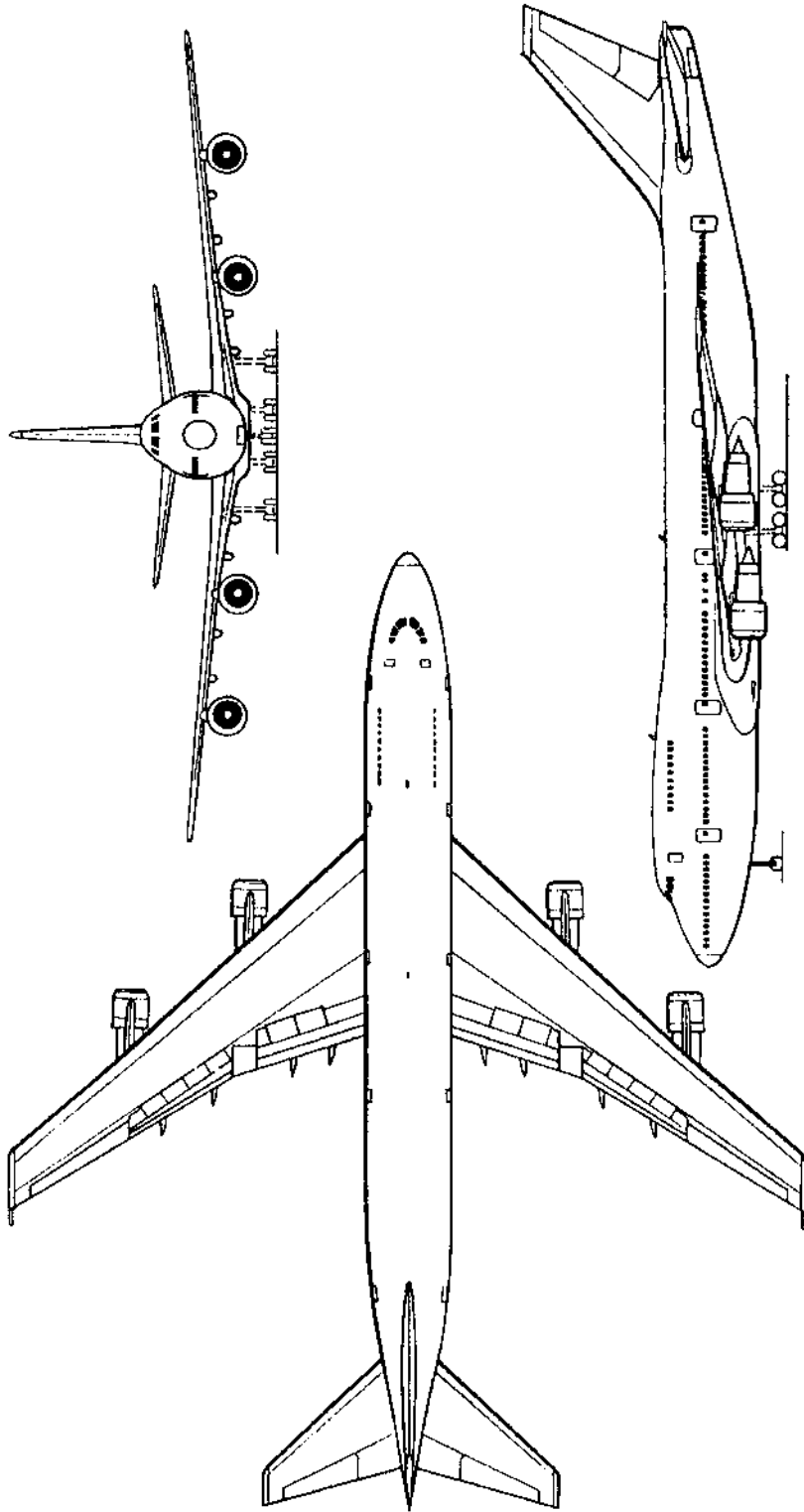


Figure 15. 747-21P configuration.

Table 6. ACSYNT variables

| Variable                                | Type    | Dimension | Description   | Units/comment             | Default (747) |
|---|---------|-----------|---|---------------------------|---------------|
| <b>1. Geometry module</b>               |         |           |   |                           |               |
| <b>Namelist WING</b>                    |         |           |   |                           |               |
| SWEEP                                   | float   | 1         | Sweep of wing.  | degrees                   | 37.17         |
| KSWEEP                                  | integer | 1         | 1 → Referenced to the leading edge.   |                           | 2             |
|   |         |           | 2 → Referenced to the quarter chord.  |                           |               |
|   |         |           | 3 → Referenced to the trailing edge.  |                           |               |
| AR                                      | float   | 1         | Aspect ratio of wing.   |                           | 6.96          |
| TAPER                                   | float   | 1         | Taper ratio of wing.  |                           | 0.2646        |
| TCROOT                                  | float   | 1         | Thickness-to-chord ratio at the root.   |                           | 0.1794        |
| TCTIP                                   | float   | 1         | Thickness-to-chord ratio at the tip.  |                           | 0.078         |
| ZROOT                                   | float   | 1         | Elevation of MAC above fuselage reference plane, measured as a fraction of the local fuselage radius.   |                           | -0.1          |
| AREA                                    | float   | 1         | Planform area of wing.  | ft <sup>2</sup>           | 5469          |
| DIHED                                   | float   | 1         | Dihedral angle of wing.   | degrees                   | 7             |
| XWING                                   | float   | 1         | Ratio of distance measured from nose to leading edge of wing to total fuselage length.  |                           | 0.249         |
| <b>Namelist HTAIL (horizontal tail)</b> |         |           |   |                           |               |
| SWEEP                                   | float   | 1         | Sweep of tail   | degrees                   | 34.29         |
| KSWEEP                                  | integer | 1         | 1 → Referenced to the leading edge.   |                           | 2             |
|   |         |           | 2 → Referenced to the quarter chord.  |                           |               |
|   |         |           | 3 → Referenced to the trailing edge.  |                           |               |
| AR                                      | float   | 1         | Aspect ratio of the horizontal wing.  | (span) <sup>2</sup> /area | 3.625         |
| TAPER                                   | float   | 1         | Taper ratio of the horizontal wing.   | tip chord/root chord      | 0.25          |
| TCROOT                                  | float   | 1         | Thickness-to-chord ratio at the root.   |                           | 0.11          |
| TCTIP                                   | float   | 1         | Thickness-to-chord ratio at the tip.  |                           | 0.08          |
| ZROOT                                   | float   | 1         | Elevation of MAC above fuselage reference plane, measured as a fraction of the local fuselage radius.   |                           | 0.69          |
| AREA                                    | float   | 1         | Planform area of the horizontal wing.   | ft <sup>2</sup>           | 1470          |
| XHTAIL                                  | float   | 1         | Position for trailing edge of tail root chord. If ZROOT ≤ 1, then XHTAIL is given as a fraction of body length. Else, XHTAIL is given as a fraction of the local vertical tail chord. |                           | 1             |



Table 6. Continued

| Variable   | Type    | Dimension | Description  | Units/comment             | Default (747) |
|--|---------|-----------|--|---------------------------|---------------|
| <b>Namelist VTAIL (vertical tail)</b>              |         |           |  |                           |               |
| SWEEP  | float   | 1         | Sweep of vertical tail.  | degrees                   | 45.73         |
| KSWEEP   | integer | 1         | 1 → Referenced to the leading edge.  |                           | 2             |
|  |         |           | 2 → Referenced to the quarter chord.   |                           |               |
|  |         |           | 3 → Referenced to the trailing edge.   |                           |               |
| AR   | float   | 1         | Aspect ratio of vertical tail.   | (span) <sup>2</sup> /area | 1.247         |
| TAPER  | float   | 1         | Taper ratio of vertical tail.  | tip chord/root chord      | 0.34          |
| TCROOT   | float   | 1         | Thickness-to-chord ratio at root.  |                           | 0.1298        |
| TCTIP  | float   | 1         | Thickness-to-chord ratio at tip.   |                           | 0.089         |
| ZROOT  | float   | 1         | Elevation of MAC above fuselage reference plane, measured as a fraction of the local fuselage radius.  |                           | 0.6           |
| AREA   | float   | 1         | Planform area of vertical tail.  | ft <sup>2</sup>           | 830           |
| <b>Namelist FUS (fuselage)</b>                     |         |           |  |                           |               |
| FRN  | float   | 1         | Fineness ratio of the nose section.  | length/diameter           | 2.13          |
| FRAB   | float   | 1         | Fineness ratio of after-body section.  | length/diameter           | 3.29          |
| BODL   | float   | 1         | Length of fuselage.  | ft                        | 225.167       |
| BDMAX  | float   | 1         | Maximum diameter of fuselage.  | ft                        | 20.2          |
| <b>Namelist WPOD (wing-mounted propulsion pod)</b> |         |           |  |                           |               |
| DIAM   | float   | 1         | Engine diameter.   | ft                        | 6.2           |
| LENGTH   | float   | 1         | Length of engine pod.  | ft                        | 15            |
| X  | float   | 1         | X location of nose of pod relative to leading edge of wing, given as a fraction of local chord of wing (>0 if face of pod is behind leading edge of wing). |                           | -0.631        |
| Y  | float   | 1         | Y location of center of pod, given as a fraction of semispan, measured from body centerline.   |                           | 0.241         |
| Z  | float   | 1         | Z location of center of pod above wing local chord, given as fraction of maximum pod diameter.   |                           | -0.83         |
| SWFACT   | float   | 1         | Wetted area multiplier.  |                           |               |

Table 6. Concluded

| Variable   | Type  | Dimension | Description   | Units/comment | Default (747) |
|--|-------|-----------|---|---------------|---------------|
| <b>Namelist FPOD (fuselage-mounted propulsion pod)</b> |       |           |   |               |               |
| DIAM   | float | 1         | Engine diameter.  | ft            | N/A           |
| LENGTH   | float | 1         | Length of engine pod.   | ft            | N/A           |
| SOD  | float | 1         | Stand-off-distance, the distance from the pod wall to the fuselage wall, given as a fraction of maximum pod radius. |               | N/A           |
| THETA  | float | 1         | Angular orientation of pod, THETA measured positive up from the horizontal reference plane.                         | degrees       | N/A           |
| X  | float | 1         | X location of nose relative to nose of fuselage, given as a fraction of body length.                                |               | N/A           |
| <b>2. Trajectory module</b>                            |       |           |   |               |               |
| <b>Namelist TRDATA (used for load factors)</b>         |       |           |   |               |               |
| DESLF  | float | 1         | Design load factor.   | N/A           | 2.5           |
| ULTLF  | float | 1         | Ultimate load factor, usually 1.5*DESLF.  | N/A           | 3.75          |
| <b>3. Weights module</b>                               |       |           |   |               |               |
| <b>Namelist OPTS</b>                                   |       |           |   |               |               |
| WGTO   | float | 1         | Gross take-off weight.  | lb            | 713000        |
| WE   | float | 1         | Total weight of propulsion system (includes both wing and fuselage mounted engines).                                | lb            | 44290         |

Table 7. PDCYL variables

| Variable                | Type    | Dimension | Description  | Units/comment                        | Default (747) |
|-------------------------|---------|-----------|--|--------------------------------------|---------------|
| <b>Namelist PDCYLIN</b> |         |           |  |                                      |               |
| <b>Wing</b>             |         |           |  |                                      |               |
| Material properties     |         |           |  |                                      |               |
| PS                      | float   | 1         | Plasticity factor.   |                                      | 1             |
| TMGW                    | float   | 1         | Min. gage thickness for the wing   | inches                               | 0.2           |
| EFFW                    | float   | 1         | Buckling efficiency of the web.  |                                      | 0.656         |
| EFFC                    | float   | 1         | Buckling efficiency of the covers.   |                                      | 1.03          |
| ESW                     | float   | 1         | Young's Modulus for wing material.   | psi                                  | 1.07E+07      |
| FCSW                    | float   | 1         | Ult. compressive strength of wing.   | psi                                  | 54000         |
| DSW                     | float   | 1         | Density of the wing material.  | lb/in. <sup>3</sup>                  | 0.101         |
| KDEW                    | float   | 1         | Knock-down factor for Young's Modulus.   |                                      | 1             |
| KDFW                    | float   | 1         | Knock-down factor for Ultimate strength.   |                                      | 1             |
| Geometric parameters    |         |           |  |                                      |               |
| ISTAMA                  | integer | 1         | 1 → the position of the wing is unknown.<br>2 → the position of the wing is known. |                                      | 2             |
| CS1                     | float   | 1         | Position of structural wing box from leading edge as percent of root chord.        |                                      | 0.088         |
| CS2                     | float   | 1         | Position of structural wing box from trailing edge as percent of root chord.       |                                      | 0.277         |
| Structural concept      |         |           |  |                                      |               |
| CLAQR                   | float   | 1         | Ratio of body lift to wing lift.   | For subsonic aircraft<br>CLAQR ~ 0.0 | 0.001         |
| IFUEL                   | integer | 1         | 1 → no fuel is stored in the wing.<br>2 → fuel is stored in the wing.              |                                      | 2             |
| CWMAN                   | float   | 1         | Design maneuver load factor.   |                                      | 1             |
| CF                      |         |           | Shanley's const. for frame bending.  |                                      | 6.25E-05      |
| <b>Fuselage</b>         |         |           |  |                                      |               |
| Structural concept      |         |           |  |                                      |               |
| CKF                     | float   | 1         | Frame stiffness coefficient.   |                                      | 5.24          |
| EC                      | float   | 1         | Power in approximation equation for buckling stability.                            |                                      | 2.36          |
| KGC                     | float   | 1         | Buckling coefficient for component general buckling of stiffener web panel.        |                                      | 0.368         |
| KGW                     | float   | 1         | Buckling coefficient for component local buckling of web panel.                    |                                      | 0.505         |

Table 7. Continued

| KCON(T/B) | Structural geometry concept  |  |  | Default (747) |
|-----------|--|--|--|---------------|
| 2         | Simply stiffened shell, frames, sized for minimum weight in buckling   |  |  |               |
| 3         | Z-stiffened shell, frames, best buckling                               |  |  |               |
| 4         | Z-stiffened shell, frames, buckling-minimum gage compromise            |  |  |               |
| 5         | Z-stiffened shell, frames, buckling-pressure compromise                |  |  | 4             |
| 6         | Truss-core sandwich, frames, best buckling                             |  |  |               |
| 8         | Truss-core sandwich, no frames, best buckling                          |  |  |               |
| 9         | Truss-core sandwich, no frames, buckling-min. gage-pressure compromise |  |  |               |

| Variable             | Type    | Dimension | Description  | Units/Comment       | Default (747) |
|----------------------|---------|-----------|--|---------------------|---------------|
| Material properties  |         |           |  |                     |               |
| FTS(T/B)             | float   | 4         | Tensile strength on (top/bottom).  | psi                 | 58500         |
| FCS(T/B)             | float   | 4         | Compressive strength.  | psi                 | 54000         |
| ES(T/B)              | float   | 4         | Young's Modulus for the shells.  | psi                 | 1.07E+07      |
| EF(T/B)              | float   | 4         | Young's Modulus for the frames.  | psi                 | 1.07E+07      |
| DS(T/B)              | float   | 4         | Density of shell material on (t/b).  | lb/in. <sup>3</sup> | 0.101         |
| DF(T/B)              | float   | 4         | Density of frame material.   | lb/in. <sup>3</sup> | 0.101         |
| TMG(T/B)             | float   | 4         | Minimum gage thickness.  | in.                 | 0.071         |
| KDE                  | float   | 1         | Knock-down factor for modulus.   |                     | 1             |
| KDF                  | float   | 1         | Knock-down factor for strength.  |                     | 1             |
| Geometric parameters |         |           |  |                     |               |
| CLBR1                | float   | 1         | Fuselage break point as a fraction of total fuselage length.   |                     | 1.1           |
| ICYL                 | integer | 1         | 1 → modeled with a mid-body cylinder.<br>Else → use two power-law bodies back to back.                           |                     | 1             |
| <b>Loads</b>         |         |           |  |                     |               |
| AXAC                 | float   | 1         | Axial acceleration.  | g's                 | 0             |
| CMAN                 | float   | 1         | Weight fraction at maneuver.   |                     | 1             |
| ILOAD                | integer | 1         | 1 → analyze maneuver only.<br>2 → analyze maneuver and landing only.<br>3 → analyze bump, landing, and maneuver. |                     | 3             |
| PG(T/B)              | float   | 12        | Fuselage gage pressure on (top/bot).   | psi                 | 13.65         |
| WFBUMP               | float   | 1         | Weight fraction at bump.   |                     | 0.001         |
| WFLAND               | float   | 1         | Weight fraction at landing.  |                     | 0.9           |

Table 7. Continued

| Variable            | Type    | Dimension | Description   | Units/Comment                         | Default (747) |
|---------------------|---------|-----------|---|---------------------------------------|---------------|
| <b>Landing gear</b> |         |           |   |                                       |               |
| VSINK               | float   | 1         | Design sink velocity at landing.  | ft/sec                                | 10            |
| STROKE              | float   | 1         | Stroke of landing gear.   | ft                                    | 2.21          |
| CLRG1               | float   | 1         | Length fraction of nose landing gear.   |                                       | 0.1131        |
| CLRG2               | float   | 1         | Length fraction of main landing gear measured as a fraction of total fuselage length. |                                       | 0.466         |
| WFGR1               | float   | 1         | Weight fraction of nose landing gear.   |                                       | 0.0047        |
| WFGR2               | float   | 1         | Weight fraction of main landing gear.   |                                       | 0.0398        |
| IGEAR               | integer | 1         | 1 → main landing gear located on fuselage.<br>2 → main landing gear located on wing.  |                                       | 2             |
| GFRL                | float   | 1         | Ratio of force taken by nose landing gear to force taken by main gear at landing.     |                                       | 0.001         |
| CLRGW1              | float   | 1         | Position of wing gear as a fraction of structural semispan.                           | If only 1 wing gear, set CLRGW2 = 0.0 | 0.064         |
| CLRGW2              | float   | 1         |   |                                       | 0.1844        |
| <b>Tails</b>        |         |           |   |                                       |               |
| ITAIL               | integer | 1         | 1 → control surfaces mounted on tail.<br>2 → control surfaces mounted on wing.        |                                       | 1             |
| <b>Weights</b>      |         |           |   |                                       |               |
| WTFF                | float   | 1         | Weight fraction of fuel.  |                                       | 0.262         |
| CBUM                | float   | 1         | Weight fraction at bump.  |                                       | 1             |
| CLAN                | float   | 1         | Weight fraction at landing.   |                                       | 0.791         |

Table 7. Concluded

| Variable       | Type    | Dimension | Description  | Units/Comment | Default (747) |
|----------------|---------|-----------|--|---------------|---------------|
| <b>Factors</b> |         |           |  |               |               |
| ISCHRENK       | integer | 1         | 1 → use Schrenk load distribution on wing.<br>Else → use trapezoidal distribution. |               | 1             |
| ICOMND         | integer | 1         | 1 → print gross shell dimensions envelope.<br>2 → print detailed shell geometry.   |               | 1             |
| WGNO           | float   | 1         | Nonoptimal factor for wing (including the secondary structure).                    |               | 1             |
| SLFMB          | float   | 1         | Static load factor for bumps.  |               | 1.2           |
| WMIS           | float   | 1         | Volume component of secondary structure.   |               | 0             |
| WSUR           | float   | 1         | Surface area component of secondary structure.                                     |               | 0             |
| WCW            | float   | 1         | Factor in weight equation for nonoptimal weights.                                  |               | 1             |
| WCA            | float   | 1         | Factor in weight equation multiplying surface areas for nonoptimal weights.        |               | 0             |
| NWING          | integer | 1         | Number of wing segments for analysis.  |               | 40            |

Table 8. Key configuration parameters for eight transport aircraft

| Variable                       | 720    | 727    | 737    | 747    | DC-8   | MD-11  | MD-83 | L-1011 |
|--------------------------------|--------|--------|--------|--------|--------|--------|-------|--------|
| <b>ACSYNT INPUT PARAMETERS</b> |        |        |        |        |        |        |       |        |
| <b>1. Geometry module</b>      |        |        |        |        |        |        |       |        |
| <b>Namelist WING</b>           |        |        |        |        |        |        |       |        |
| SWEEP                          | 35     | 32     | 25     | 37.17  | 30.6   | 35     | 24.16 | 35     |
| KSWEEP                         | 2      | 2      | 2      | 2      | 2      | 2      | 2     | 2      |
| AR                             | 6.958  | 7.67   | 8.21   | 6.96   | 7.52   | 7.5    | 9.62  | 6.98   |
| TAPER                          | 0.333  | 0.2646 | 0.2197 | 0.2646 | 0.1974 | 0.255  | 0.156 | 0.3    |
| TCROOT                         | 0.1551 | 0.154  | 0.126  | 0.1794 | 0.1256 | 0.167  | 0.138 | 0.13   |
| TCTIP                          | 0.0902 | 0.09   | 0.112  | 0.078  | 0.105  | 0.093  | 0.12  | 0.09   |
| ZROOT                          | -1     | -1     | -0.25  | -0.1   | -1     | -0.79  | -1    | -1     |
| AREA                           | 2460   | 1587   | 1005   | 5469   | 2927   | 3648   | 1270  | 3590   |
| DIHED                          | 3      | 3      | 6      | 7      | 3      | 6      | 3     | 3      |
| XWING                          | 0.2963 | 0.376  | 0.35   | 0.249  | 0.302  | 0.218  | 0.468 | 0.359  |
| <b>Namelist HTAIL</b>          |        |        |        |        |        |        |       |        |
| SWEEP                          | 35     | 31.05  | 30.298 | 34.29  | 35     | 35.5   | 30.8  | 3.5    |
| KSWEEP                         | 2      | 2      | 2      | 2      | 2      | 2      | 2     | 2      |
| AR                             | 3.15   | 3.4    | 4.04   | 3.625  | 4.04   | 3.43   | 4.88  | 4      |
| TAPER                          | 0.457  | 0.383  | 0.3974 | 0.25   | 0.329  | 0.412  | 0.357 | 0.33   |
| TCROOT                         | 0.11   | 0.11   | 0.132  | 0.11   | 0.095  | 0.143  | 0.107 | 0.095  |
| TCTIP                          | 0.09   | 0.0894 | 0.108  | 0.08   | 0.08   | 0.1067 | 0.08  | 0.08   |
| ZROOT                          | 0.5    | 2      | 0.67   | 0.69   | 0.25   | 0.6875 | 2     | 0.5    |
| AREA                           | 500    | 376    | 312    | 1470   | 559    | 920    | 314   | 1282   |
| XHTAIL                         | 1      | 0.95   | 0.8532 | 0.974  | 1      | 0.96   | 0.98  | 0.9265 |
| <b>Namelist VTAIL</b>          |        |        |        |        |        |        |       |        |
| SWEEP                          | 35     | 48.4   | 34.16  | 45.73  | 35     | 38     | 39.4  | 35     |
| KSWEEP                         | 2      | 2      | 2      | 2      | 2      | 2      | 2     | 2      |
| AR                             | 1.45   | 1.09   | 1.814  | 1.247  | 1.905  | 1.73   | 1.48  | 1.6    |
| TAPER                          | 0.484  | 0.641  | 0.3024 | 0.34   | 0.292  | 0.343  | 0.844 | 0.3    |
| TCROOT                         | 0.11   | 0.11   | 0.1322 | 0.1298 | 0.096  | 0.105  | 0.127 | 0.11   |
| TCTIP                          | 0.0896 | 0.09   | 0.1081 | 0.089  | 0.101  | 0.125  | 0.103 | 0.0896 |
| ZROOT                          | 0.95   | 0.2    | 0      | 0.6    | 0.95   | 0.85   | 0.9   | 0.95   |
| AREA                           | 312.4  | 356    | 225    | 830    | 352    | 605    | 550   | 550    |

Table 8. Continued

| Variable                            | 720   | 727    | 737    | 747     | DC-8   | MD-11   | MD-83 | L-1011 |
|-------------------------------------|-------|--------|--------|---------|--------|---------|-------|--------|
| <b>Namelist FUS</b>                 |       |        |        |         |        |         |       |        |
| FRN                                 | 1.81  | 2      | 1.915  | 2.13    | 2      | 1.67    | 1.15  | 1.76   |
| FRAB                                | 2.86  | 2.831  | 2.361  | 3.29    | 2.9375 | 2.27    | 2.73  | 2.96   |
| BODL                                | 130.5 | 116.67 | 90.58  | 225.167 | 153    | 192.42  | 135.5 | 177.67 |
| BDMAX                               | 14.21 | 14.2   | 13.167 | 20.2    | 13.5   | 19.75   | 11.44 | 19.583 |
| <b>Namelist WPOD (inboard)</b>      |       |        |        |         |        |         |       |        |
| DIAM                                | 3.24  | N/A    | 3.542  | 6.2     | 4.42   | 9.04    | N/A   | 3.24   |
| LENGTH                              | 12.15 | N/A    | 10     | 15      | 12.15  | 18.08   | N/A   | 12.15  |
| X                                   | 0.917 | N/A    | -0.22  | -0.631  | -0.4   | -0.558  | N/A   | -0.639 |
| Y                                   | 0.386 | N/A    | 0.343  | 0.241   | 0.352  | 0.33125 | N/A   | 0.461  |
| Z                                   | -1    | N/A    | -0.548 | -0.83   | -1.2   | -0.5    | N/A   | -1     |
| SWFACT                              | 1     | N/A    | 1      | 1       | 1      | 1       | N/A   | 1      |
| <b>Namelist WPOD (outboard)</b>     |       |        |        |         |        |         |       |        |
| DIAM                                | 3.24  | N/A    | N/A    | 6.2     | 4.42   | N/A     | N/A   | N/A    |
| LENGTH                              | 12.15 | N/A    | N/A    | 15      | 12.15  | N/A     | N/A   | N/A    |
| X                                   | 0.917 | N/A    | N/A    | -0.631  | -0.955 | N/A     | N/A   | N/A    |
| Y                                   | 0.674 | N/A    | N/A    | 0.441   | 0.61   | N/A     | N/A   | N/A    |
| Z                                   | -1    | N/A    | N/A    | -0.83   | -1.2   | N/A     | N/A   | N/A    |
| SWFACT                              | 1     | N/A    | N/A    | 1       | 1      | N/A     | N/A   | N/A    |
| <b>Namelist FPOD</b>                |       |        |        |         |        |         |       |        |
| DIAM                                | N/A   | 3.542  | N/A    | N/A     | N/A    | 9.04    | 6.6   | 3.24   |
| LENGTH                              | N/A   | 10     | N/A    | N/A     | N/A    | 40.68   | 20.34 | 12.15  |
| SOD                                 | N/A   | 0      | N/A    | N/A     | N/A    | 0       | 0     | 0      |
| THETA                               | N/A   | 90     | N/A    | N/A     | N/A    | 90      | 0     | 90     |
| X                                   | N/A   | 0.699  | N/A    | N/A     | N/A    | 0.812   | 0.746 | 0.725  |
| SYMCOD                              | N/A   | 1      | N/A    | N/A     | N/A    | 1       | 0     | -1     |
| <b>Namelist FPOD (third engine)</b> |       |        |        |         |        |         |       |        |
| DIAM                                | N/A   | 3.542  | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |
| LENGTH                              | N/A   | 10     | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |
| SOD                                 | N/A   | 0.2    | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |
| THETA                               | N/A   | 14.8   | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |
| X                                   | N/A   | 0.699  | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |
| SYMCOD                              | N/A   | 0      | N/A    | N/A     | N/A    | N/A     | N/A   | N/A    |



Table 8. Continued

| Variable                      | 720      | 727      | 737      | 747      | DC-8     | MD-11    | MD-83    | L-1011   |
|-------------------------------|----------|----------|----------|----------|----------|----------|----------|----------|
| <b>2. Trajectory module</b>   |          |          |          |          |          |          |          |          |
| <b>Namelist TRDATA</b>        |          |          |          |          |          |          |          |          |
| DESLF                         | 2.5      | 2.5      | 2.5      | 2.5      | 2.5      | 2.5      | 2.5      | 2.5      |
| ULTLF                         | 3.75     | 3.75     | 3.75     | 3.75     | 3.75     | 3.75     | 3.75     | 3.75     |
| <b>3. Weights module</b>      |          |          |          |          |          |          |          |          |
| <b>Namelist OPTS</b>          |          |          |          |          |          |          |          |          |
| WGTO                          | 202000   | 160000   | 100800   | 713000   | 335000   | 602500   | 140000   | 409000   |
| <b>Namelist FIXW</b>          |          |          |          |          |          |          |          |          |
| WE                            | 18202    | 12759    | 8165     | 44290    | 27058    | 40955    | 10340    | 34797    |
| <b>PDCYL INPUT PARAMETERS</b> |          |          |          |          |          |          |          |          |
| <b>Wing</b>                   |          |          |          |          |          |          |          |          |
| Geometric parameters          |          |          |          |          |          |          |          |          |
| ISTAMA                        | 2        | 2        | 2        | 2        | 2        | 2        | 2        | 2        |
| CS1                           | 0.1      | 0.2125   | 0.0724   | 0.088    | 0.0818   | 0.168    | 0.181    | 0.093    |
| CS2                           | 0.27     | 0.25     | 0.238    | 0.277    | 0.136    | 0.2835   | 0.271    | 0.296    |
| Structural concept            |          |          |          |          |          |          |          |          |
| CLAQR                         | 0.001    | 0.001    | 0.001    | 0.001    | 0.001    | 0.001    | 0.001    | 0.001    |
| IFUEL                         | 2        | 2        | 2        | 2        | 2        | 2        | 2        | 2        |
| CWMAN                         | 1        | 1        | 1        | 1        | 1        | 1        | 1        | 1        |
| CF                            | 6.25E-05 | 6.25E-05 | 6.25E-05 | 6.25E-05 | 6.25E-05 | 6.25E-05 | 6.25E-05 | 6.25E-05 |
| Material properties           |          |          |          |          |          |          |          |          |
| PS                            | 1        | 1        | 1        | 1        | 1        | 1        | 1        | 1        |
| TMGW                          | 0.02     | 0.02     | 0.02     | 0.02     | 0.02     | 0.02     | 0.02     | 0.02     |
| EFFW                          | 0.656    | 0.656    | 0.656    | 0.656    | 0.656    | 0.656    | 0.656    | 0.656    |
| EFFC                          | 1.03     | 1.03     | 1.03     | 1.03     | 1.03     | 1.03     | 1.03     | 1.03     |
| ESW                           | 1.08E+07 | 1.08E+07 | 1.08E+07 | 1.07E+07 | 1.08E+07 | 1.07E+07 | 1.07E+07 | 1.06E+07 |
| FCSW                          | 63500    | 56000    | 56000    | 54000    | 56000    | 56000    | 56000    | 67000    |
| DSW                           | 0.101    | 0.101    | 0.101    | 0.101    | 0.101    | 0.101    | 0.101    | 0.101    |
| KDEW                          | 1        | 1        | 1        | 1        | 1        | 1        | 1        | 1        |
| KDFW                          | 1        | 1        | 1        | 1        | 1        | 1        | 1        | 1        |

Table 8. Continued

| <b>Variable</b>      | <b>720</b> | <b>727</b> | <b>737</b> | <b>747</b> | <b>DC-8</b> | <b>MD-11</b> | <b>MD-83</b> | <b>L-1011</b> |
|----------------------|------------|------------|------------|------------|-------------|--------------|--------------|---------------|
| <b>Fuselage</b>      |            |            |            |            |             |              |              |               |
| Geometric parameters |            |            |            |            |             |              |              |               |
| CLBR1                | 1.1        | 1.1        | 1.1        | 1.1        | 1.1         | 1.1          | 1.1          | 1.1           |
| ICYL                 | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| Structural concept   |            |            |            |            |             |              |              |               |
| CKF                  | 5.24       | 5.24       | 5.24       | 5.24       | 5.24        | 5.24         | 5.24         | 5.24          |
| EC                   | 2.36       | 2.36       | 2.36       | 2.36       | 2.36        | 2.36         | 2.36         | 2.36          |
| KGC                  | 0.368      | 0.368      | 0.368      | 0.368      | 0.368       | 0.368        | 0.368        | 0.368         |
| KGW                  | 0.505      | 0.505      | 0.505      | 0.505      | 0.505       | 0.505        | 0.505        | 0.505         |
| Material properties  |            |            |            |            |             |              |              |               |
| FTS(T/B)             | 58500      | 58500      | 58500      | 58500      | 64000       | 58500        | 58500        | 58500         |
| FCS(T/B)             | 54000      | 54000      | 54000      | 54000      | 39000       | 54000        | 54000        | 54000         |
| ES(T/B)              | 1.07E+07   | 1.07E+07   | 1.07E+07   | 1.07E+07   | 1.07E+07    | 1.07E+07     | 1.07E+07     | 1.07E+07      |
| EF(T/B)              | 1.07E+07   | 1.07E+07   | 1.07E+07   | 1.07E+07   | 1.07E+07    | 1.07E+07     | 1.07E+07     | 1.07E+07      |
| DS(T/B)              | 0.101      | 0.101      | 0.101      | 0.101      | 0.101       | 0.101        | 0.101        | 0.101         |
| DF(T/B)              | 0.101      | 0.101      | 0.101      | 0.101      | 0.101       | 0.101        | 0.101        | 0.101         |
| TMG(T/B)             | 0.04       | 0.04       | 0.036      | 0.071      | 0.05        | 0.055        | 0.055        | 0.075         |
| KDE                  | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| KDF                  | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| <b>Loads</b>         |            |            |            |            |             |              |              |               |
| AXAC                 | 0          | 0          | 0          | 0          | 0           | 0            | 0            | 0             |
| CMAN                 | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| ILOAD                | 3          | 3          | 3          | 3          | 3           | 3            | 3            | 3             |
| PG(T/B)              | 12.9       | 12.9       | 11.25      | 13.65      | 13.155      | 11.5         | 12.5         | 12.6          |
| WFBUMP               | 0.001      | 0.001      | 0.001      | 0.001      | 0.001       | 0.001        | 0.001        | 0.001         |
| WFLAND               | 0.9        | 0.9        | 0.9        | 0.9        | 0.9         | 0.9          | 0.9          | 0.9           |

Table 8. Concluded

| <b>Variable</b>     | <b>720</b> | <b>727</b> | <b>737</b> | <b>747</b> | <b>DC-8</b> | <b>MD-11</b> | <b>MD-83</b> | <b>L-1011</b> |
|---------------------|------------|------------|------------|------------|-------------|--------------|--------------|---------------|
| <b>Landing gear</b> |            |            |            |            |             |              |              |               |
| VSINK               | 10         | 10         | 10         | 10         | 10          | 10           | 10           | 10            |
| STROKE              | 1.67       | 1.167      | 1.167      | 2.21       | 1.375       | 1.9          | 1.67         | 2.17          |
| CLRG1               | 0.133      | 0.1306     | 0.145      | 0.1131     | 0.108       | 0.141        | 0.055        | 0.161         |
| CLRG2               | 0.51       | 0.5896     | 0.5254     | 0.466      | 0.499       | 0.57         | 0.597        | 0.56          |
| WFG1                | 0.00389    | 0.00725    | 0.0052     | 0.0047     | 0.0311      | 0.0031       | 0.004        | 0.005         |
| WFG2                | 0.036      | 0.0738     | 0.0382     | 0.0398     | 0.0742      | 0.0058       | 0.035        | 0.044         |
| IGEAR               | 2          | 2          | 2          | 2          | 2           | 2            | 2            | 2             |
| GFRL                | 0.001      | 0.001      | 0.001      | 0.001      | 0.001       | 0.001        | 0.001        | 0.001         |
| CLRGW1              | 0.1675     | 0.1736     | 0.1846     | 0.064      | 0.14        | 0.2          | 0.148        | 0.232         |
| CLRGW2              | 0          | 0          | 0          | 0.1844     | 0           | 0            | 0            | 0             |
| <b>Tails</b>        |            |            |            |            |             |              |              |               |
| ITAIL               | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| <b>Weights</b>      |            |            |            |            |             |              |              |               |
| WTFF                | 0.3263     | 0.2625     | 0.156      | 0.262      | 0.418       | 0.336        | 0.2795       | 0.246         |
| CBUM                | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| CLAN                | 0.813      | 0.859      | 0.972      | 0.791      | 0.7164      | 0.7137       | 0.9143       | 0.851         |
| <b>Factors</b>      |            |            |            |            |             |              |              |               |
| ISCHRENK            | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| ICOMND              | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| WGNO                | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| SLFMB               | 1.2        | 1.2        | 1.2        | 1.2        | 1.2         | 1.2          | 1.2          | 1.2           |
| WMIS                | 0          | 0          | 0          | 0          | 0           | 0            | 0            | 0             |
| WSUR                | 0          | 0          | 0          | 0          | 0           | 0            | 0            | 0             |
| WCW                 | 1          | 1          | 1          | 1          | 1           | 1            | 1            | 1             |
| WCA                 | 0          | 0          | 0          | 0          | 0           | 0            | 0            | 0             |
| NWING               | 40         | 40         | 40         | 40         | 40          | 40           | 40           | 40            |

\$PDCYLIN

|   |  |   |                             |
|---|--|---|-----------------------------|
| PS=1.,<br>EFFC=1.03,<br>KDEW=1.0,   | TMGW=.02,<br>ESW=10.7E06,<br>KDFW=1.0,           | EFFW=.656,<br>FCSW=54000.,  | DSW=0.101,                  |
| ISTAMA=2,   | CS1=0.088,                                       | CS2=0.277,  |                             |
| CLAQR=.001,<br>CKF=5.24,  | IFUEL=2,<br>EC=2.36,                             | CWMAN=1.0,<br>KGC=.368,   | CF=6.25E-05,<br>KGW=.505,   |
| FTST = 4*58500.,8*0.,<br>FCST = 4*54000.,8*0.,<br>EST = 4*10.70E06,8*0.,<br>EFT = 4*10.70E06,8*0.,<br>DST = 4*.101,8*0.,<br>DFT = 4*.101,8*0.,<br>TMGT = 4*.071,8*0.,<br>KDE = 0.9, |  | FTSB = 4*58500.,8*0.,<br>FCSB = 4*54000.,8*0.,<br>ESB = 4*10.70E06,8*0.,<br>EFB = 4*10.70E06,8*0.,<br>DSB = 4*.101,8*0.,<br>DFB = 4*.101,8*0.,<br>TMGB = 4*.071,8*0.,<br>KDF = 0.9, |                             |
| CLBR1=1.1,  | ICYL = 1,  |   |                             |
| KCONT = 12*4,   | KCONB = 12*4,                                    |   |                             |
| AXAC=0.,<br>CMAN=1.0,<br>WFBUMP=0.001,  | CBUM=1.0,<br>ILOAD=3,<br>WFLAND=0.9,             | CLAN=0.791,<br>PGB = 12*13.65,  | PGT = 12*13.65,             |
| WTFF=0.262,   |  |   |                             |
| VSINK=10.0,<br>WFGR1=0.0047,<br>CLRGW1=0.064,   | STROKE=2.21,<br>WFGR2=0.0398,<br>CLRGW2 =0.1844, | CLRG1=.1131,<br>IGEAR=2,  | CLRG2=0.466,<br>GFRL=0.001, |
| ITAIL=1,  |  |   |                             |
| ISCHRENK=1,<br>WMIS=0.,<br>NWING=40,  | ICOMND=1,<br>WSUR=0.,                            | WGNO=1.00,<br>WCW=1.0,  | SLFMB=1.2,<br>WCA=0.0,      |

\$END

Figure 16. PDCYLIN namelist for 747-21P.



| FUSE<br>STAT<br>FT | BENDING<br>MOMENT<br>FT.LBS | THIC<br>STRESS<br>IN | SHELL<br>THICK<br>PSI | EQUIV<br>THICK<br>IN | GAGE<br>SPACE<br>IN | FRAME<br>AREA<br>IN | NJ<br>UNITWT | SECTION<br>SQFT | SHELL<br>UNITWT<br>LB/FT2 | FRAME<br>BENDING<br>LB/FT2 | MAX<br>TYPE |
|--------------------|-----------------------------|----------------------|-----------------------|----------------------|---------------------|---------------------|--------------|-----------------|---------------------------|----------------------------|-------------|
| 3.7528             | 4516.695                    | 0.0000               | 44.5238               | 0.1448               | 0.0710              | 23797.0703          | 3            | 58.3945         | 2.1055                    | 0.0000                     | MAN         |
| 7.5056             | 29328.754                   | 0.0000               | 178.2442              | 0.1448               | 0.0710              | 5944.2905           | 3            | 94.7155         | 2.1055                    | 0.0000                     | MAN         |
| 11.2584            | 87603.664                   | 0.0000               | 401.2114              | 0.1448               | 0.0710              | 2640.8411           | 3            | 125.6875        | 2.1055                    | 0.0000                     | MAN         |
| 15.0111            | 190409.281                  | 0.0000               | 713.4453              | 0.1448               | 0.0710              | 1485.0968           | 3            | 153.6281        | 2.1055                    | 0.0001                     | MAN         |
| 18.7639            | 347701.844                  | 0.0000               | 1114.9587             | 0.1448               | 0.0710              | 950.2913            | 3            | 179.5111        | 2.1055                    | 0.0002                     | MAN         |
| 22.5167            | 568694.500                  | 0.0000               | 1605.7603             | 0.1448               | 0.0710              | 659.8342            | 3            | 203.8644        | 2.1055                    | 0.0005                     | MAN         |
| 26.2695            | 872144.000                  | 0.0000               | 2211.4465             | 0.1448               | 0.0710              | 479.1142            | 3            | 227.0152        | 2.1055                    | 0.0010                     | MAN         |
| 30.0223            | 1293259.875                 | 0.0000               | 2987.5078             | 0.1448               | 0.0710              | 354.6553            | 3            | 249.1838        | 2.1055                    | 0.0020                     | MAN         |
| 33.7751            | 1802858.500                 | 0.0000               | 3836.1211             | 0.1448               | 0.0710              | 276.1997            | 3            | 270.5282        | 2.1055                    | 0.0037                     | MAN         |
| 37.5278            | 2408529.000                 | 0.0000               | 4761.6157             | 0.1448               | 0.0710              | 222.5160            | 3            | 291.1660        | 2.1055                    | 0.0061                     | MAN         |
| 41.2806            | 3117610.000                 | 0.0000               | 5766.8906             | 0.1448               | 0.0710              | 183.7273            | 3            | 311.1883        | 2.1055                    | 0.0095                     | MAN         |
| 45.0334            | 3937044.500                 | 0.0000               | 7075.2378             | 0.1448               | 0.0710              | 149.7526            | 3            | 320.3114        | 2.1055                    | 0.0147                     | MAN         |
| 48.7862            | 4870150.000                 | 0.0000               | 8752.1152             | 0.1448               | 0.0710              | 121.0605            | 3            | 320.3114        | 2.1055                    | 0.0225                     | MAN         |
| 52.5390            | 5917042.000                 | 0.0000               | 10633.4785            | 0.1448               | 0.0710              | 99.6415             | 3            | 320.3114        | 2.1055                    | 0.0332                     | MAN         |
| 56.2918            | 7077723.000                 | 0.0000               | 12719.3301            | 0.1448               | 0.0710              | 83.3012             | 3            | 320.3114        | 2.1055                    | 0.0476                     | MAN         |
| 60.0445            | 8352191.000                 | 0.0000               | 15009.6689            | 0.1448               | 0.0710              | 70.5902             | 3            | 320.3114        | 2.1055                    | 0.0662                     | MAN         |
| 63.7973            | 9740450.000                 | 0.0000               | 17504.5000            | 0.1448               | 0.0710              | 60.5293             | 3            | 320.3114        | 2.1055                    | 0.0901                     | MAN         |
| 67.5501            | 1171814.000                 | 0.0000               | 21059.6289            | 0.1448               | 0.0710              | 50.3112             | 3            | 320.3114        | 2.1055                    | 0.1304                     | MAN         |
| 71.3029            | 15602571.000                | 0.0000               | 28039.2813            | 0.1448               | 0.0710              | 37.7875             | 3            | 320.3114        | 2.1055                    | 0.2311                     | MAN         |
| 75.0557            | 20633438.000                | 0.0000               | 37080.2188            | 0.1448               | 0.0710              | 28.5741             | 3            | 320.3114        | 2.1055                    | 0.4042                     | MAN         |
| 78.8085            | 25873488.000                | 0.0000               | 46497.0820            | 0.1448               | 0.0710              | 22.7871             | 3            | 320.3114        | 2.1055                    | 0.6356                     | MAN         |
| 82.5612            | 30384872.000                | 0.0000               | 47662.5430            | 0.1659               | 0.0813              | 25.4677             | 6            | 320.3114        | 2.4122                    | 0.5829                     | MAN         |
| 86.3140            | 33229772.000                | 0.0000               | 48052.2500            | 0.1799               | 0.0882              | 27.4022             | 6            | 320.3114        | 2.6166                    | 0.5462                     | MAN         |
| 90.0668            | 33470324.000                | 0.0000               | 48082.4258            | 0.1811               | 0.0888              | 27.5660             | 6            | 320.3114        | 2.6339                    | 0.5433                     | MAN         |
| 93.8196            | 30972306.000                | 0.0000               | 47748.3359            | 0.1688               | 0.0828              | 25.8668             | 6            | 320.3114        | 2.4544                    | 0.5750                     | MAN         |
| 97.5724            | 28304028.000                | 0.0000               | 47332.9063            | 0.1556               | 0.0763              | 24.0551             | 6            | 320.3114        | 2.2626                    | 0.6129                     | MAN         |
| 101.3252           | 25749524.000                | 0.0000               | 46274.3086            | 0.1448               | 0.0710              | 22.8968             | 3            | 320.3114        | 2.1055                    | 0.6295                     | MAN         |
| 105.0780           | 23308814.000                | 0.0000               | 41888.1211            | 0.1448               | 0.0710              | 25.2944             | 3            | 320.3114        | 2.1055                    | 0.5158                     | MAN         |
| 108.8307           | 20981884.000                | 0.0000               | 37706.4102            | 0.1448               | 0.0710              | 28.0996             | 3            | 320.3114        | 2.1055                    | 0.4180                     | MAN         |
| 112.5835           | 18768758.000                | 0.0000               | 33729.2148            | 0.1448               | 0.0710              | 31.4130             | 3            | 320.3114        | 2.1055                    | 0.3344                     | MAN         |
| 116.3363           | 16843416.000                | 0.0000               | 30269.1953            | 0.1448               | 0.0710              | 35.0038             | 3            | 320.3114        | 2.1055                    | 0.2693                     | LAN         |
| 120.0891           | 15216945.000                | 0.0000               | 27346.2754            | 0.1448               | 0.0710              | 38.7451             | 3            | 320.3114        | 2.1055                    | 0.2198                     | LAN         |
| 123.8419           | 13674075.000                | 0.0000               | 24573.5938            | 0.1448               | 0.0710              | 43.1168             | 3            | 320.3114        | 2.1055                    | 0.1775                     | LAN         |
| 127.5947           | 12214827.000                | 0.0000               | 21951.1875            | 0.1448               | 0.0710              | 48.2678             | 3            | 320.3114        | 2.1055                    | 0.1417                     | LAN         |
| 131.3474           | 10839192.000                | 0.0000               | 19479.0430            | 0.1448               | 0.0710              | 54.3936             | 3            | 320.3114        | 2.1055                    | 0.1115                     | LAN         |
| 135.1002           | 9547162.000                 | 0.0000               | 17157.1445            | 0.1448               | 0.0710              | 61.7548             | 3            | 320.3114        | 2.1055                    | 0.0865                     | LAN         |
| 138.8530           | 8338768.500                 | 0.0000               | 14985.5488            | 0.1448               | 0.0710              | 70.7038             | 3            | 320.3114        | 2.1055                    | 0.0660                     | LAN         |
| 142.6058           | 7213962.000                 | 0.0000               | 12964.1660            | 0.1448               | 0.0710              | 81.7280             | 3            | 320.3114        | 2.1055                    | 0.0494                     | LAN         |
| 146.3586           | 6172785.000                 | 0.0000               | 11093.0723            | 0.1448               | 0.0710              | 95.5133             | 3            | 320.3114        | 2.1055                    | 0.0362                     | LAN         |

Figure 18. PDCYL fuselage weight output for 747-21P.

|          |             |        |           |        |        |           |   |          |        |        |      |
|----------|-------------|--------|-----------|--------|--------|-----------|---|----------|--------|--------|------|
| 150.1113 | 5215206.000 | 0.0000 | 9372.2129 | 0.1448 | 0.0710 | 113.0507  | 3 | 320.3114 | 2.1055 | 0.0258 | LAN  |
| 153.8641 | 4341246.000 | 0.0000 | 7801.6255 | 0.1448 | 0.0710 | 135.8096  | 3 | 320.3114 | 2.1055 | 0.0179 | LAN  |
| 157.6169 | 3550887.000 | 0.0000 | 6381.2769 | 0.1448 | 0.0710 | 166.0382  | 3 | 320.3114 | 2.1055 | 0.0120 | LAN  |
| 161.3697 | 2837451.000 | 0.0000 | 5246.6328 | 0.1448 | 0.0710 | 201.9458  | 3 | 311.3084 | 2.1055 | 0.0079 | LAN  |
| 165.1224 | 2213004.000 | 0.0000 | 4268.8013 | 0.1448 | 0.0710 | 248.2045  | 3 | 298.4142 | 2.1055 | 0.0050 | LAN  |
| 168.8752 | 1666440.000 | 0.0000 | 3362.5671 | 0.1448 | 0.0710 | 315.0972  | 3 | 285.2738 | 2.1055 | 0.0030 | LAN  |
| 172.6280 | 1307928.000 | 0.0000 | 2769.3157 | 0.1448 | 0.0710 | 382.5983  | 3 | 271.8658 | 2.1055 | 0.0019 | BUM  |
| 176.3808 | 1530244.500 | 0.0000 | 3411.9824 | 0.1448 | 0.0710 | 310.5337  | 3 | 258.1649 | 2.1055 | 0.0028 | MAN  |
| 180.1335 | 1753683.000 | 0.0000 | 4134.7847 | 0.1448 | 0.0710 | 256.2493  | 3 | 244.1414 | 2.1055 | 0.0038 | MAN  |
| 183.8863 | 1890422.250 | 0.0000 | 4736.1792 | 0.1448 | 0.0710 | 223.7110  | 3 | 229.7597 | 2.1055 | 0.0047 | MAN  |
| 187.6391 | 1945607.250 | 0.0000 | 5209.6304 | 0.1448 | 0.0710 | 203.3802  | 3 | 214.9767 | 2.1055 | 0.0054 | MAN  |
| 191.3919 | 1924485.000 | 0.0000 | 5546.1831 | 0.1448 | 0.0710 | 191.0387  | 3 | 199.7393 | 2.1055 | 0.0056 | MAN  |
| 195.1447 | 1832528.250 | 0.0000 | 5733.5396 | 0.1448 | 0.0710 | 184.7960  | 3 | 183.9802 | 2.1055 | 0.0056 | MAN  |
| 198.8974 | 1675338.750 | 0.0000 | 5753.5972 | 0.1448 | 0.0710 | 184.1518  | 3 | 167.6125 | 2.1055 | 0.0051 | MAN  |
| 202.6502 | 1458795.000 | 0.0000 | 5578.8437 | 0.1448 | 0.0710 | 189.9203  | 3 | 150.5197 | 2.1055 | 0.0043 | MAN  |
| 206.4030 | 1188949.500 | 0.0000 | 5163.7246 | 0.1448 | 0.0710 | 205.1882  | 3 | 132.5389 | 2.1055 | 0.0032 | MAN  |
| 210.1558 | 872269.500  | 0.0000 | 4426.6021 | 0.1448 | 0.0710 | 239.3564  | 3 | 113.4288 | 2.1055 | 0.0020 | MAN  |
| 213.9085 | 515652.000  | 0.0000 | 3198.5554 | 0.1448 | 0.0710 | 331.2544  | 3 | 92.7996  | 2.1055 | 0.0009 | MAN  |
| 217.6613 | 126475.500  | 0.0000 | 1041.0522 | 0.1448 | 0.0710 | 1017.7543 | 3 | 69.9322  | 2.1055 | 0.0001 | MAN  |
| 221.4141 | 46821.000   | 0.0000 | 625.1013  | 0.1448 | 0.0710 | 1694.9822 | 3 | 43.1155  | 2.1055 | 0.0000 | MAN  |
| 221.4141 | 45793.500   | 0.0000 | 611.3832  | 0.1448 | 0.0710 | 1694.9822 | 3 | 43.1155  | 2.1055 | 0.0000 | NONE |

STRUCTURAL WEIGHT SUMMARY

|         | WEIGHT<br>(LBS) | WEIGHT<br>FRACTION | WEIGHT<br>UNIT |
|---------|-----------------|--------------------|----------------|
| SHELL   | 26671.41        | 0.0374             | 2.1409         |
| FRAMES  | 1837.49         | 918.7455           | 0.1475         |
| NONOP   | 0.00            | 0.0000             | 0.0000         |
| SEC     | 0.00            | 0.0000             | 0.0000         |
| TOTAL   | 28508.89        | 0.0400             | 2.2884         |
| VOLPEN  | 0.00            | 0.0000             | 0.0000         |
| GRANTOT | 28508.89        | 0.0400             | 2.2884         |

Surface Area, SQF                   12457.98  
Volume Ratio                   1.000000000  
BODY WEIGHT           28508.89453125

Figure 18. Concluded.

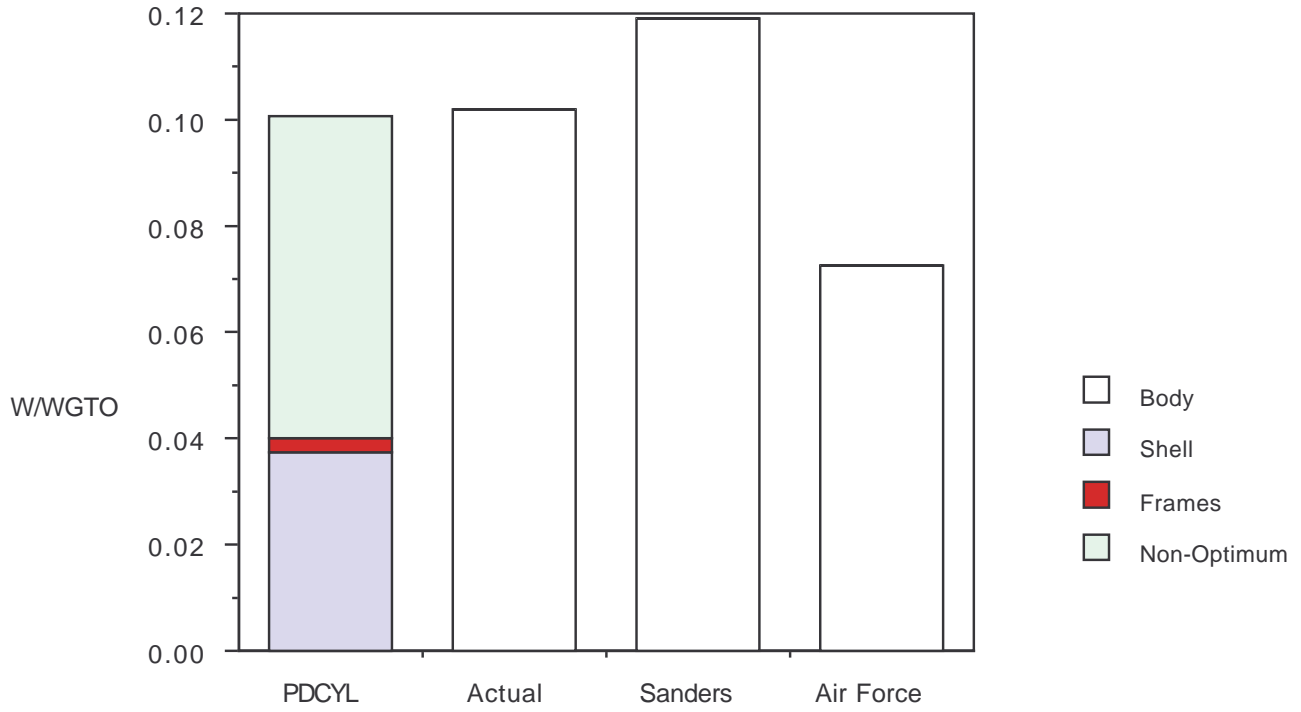


Figure 19(a). Fuselage weight estimation comparison for 747-21P.

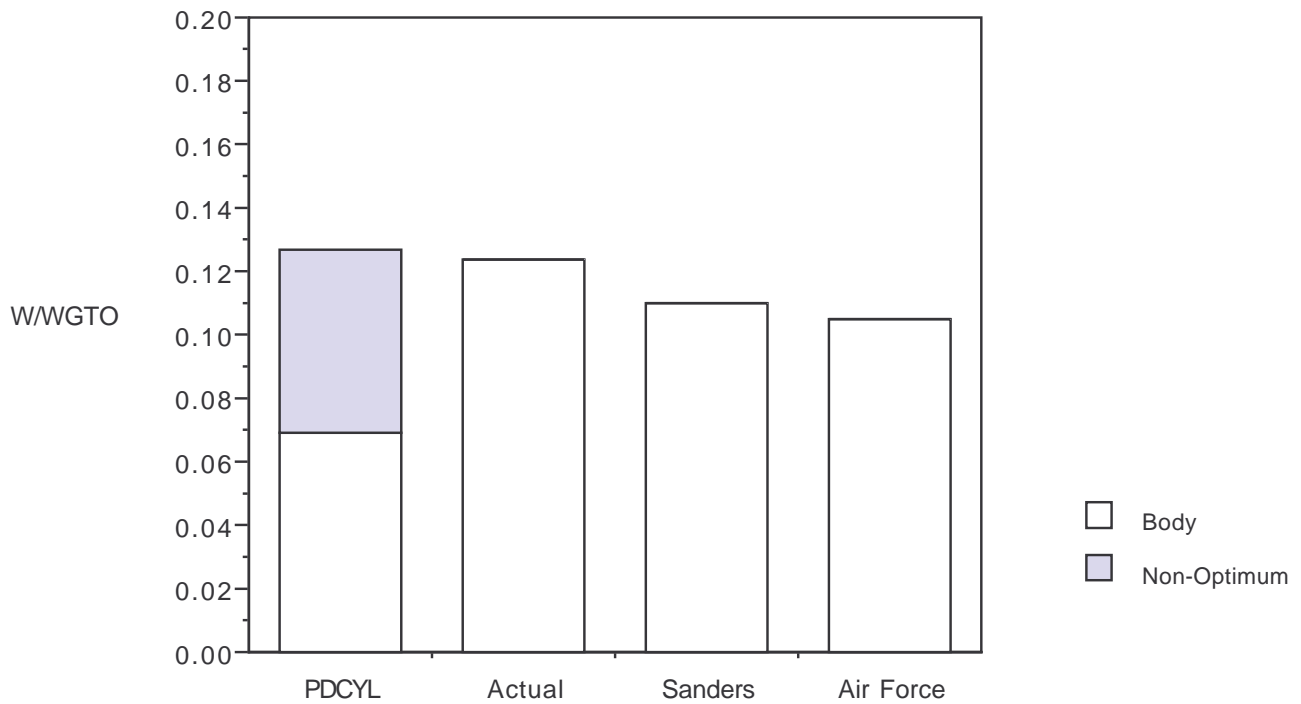


Figure 19(b). Wing weight estimation comparison for 747-21P.



## Appendix B – High-Altitude Study

### Description

A study was made to estimate the wing weight of a scaled version of an existing propeller-driven high-altitude drone aircraft. This aircraft, termed the Strato7, is modeled as an enlarged version of the existing Perseus-a3. PDCYL was used to validate the wing weight estimation returned by ACSYNT.

The wing of the Strato7 incorporates a single hollow, cylindrical carbon-fiber/epoxy spar placed at the leading edge. The strength of the cover is assumed negligible. No fuel is carried in the wing, while propulsion and landing gear are mounted on the fuselage. The layout of the Strato7 is shown in figure 20.

### Input

Fuselage weight estimation is not considered for the Strato7. An example of the ACSYNT input for the Strato7 wing weight estimation is shown in figure 21. The corresponding PDCYLIN namelist for the case where the ratio of structural chord to total chord is 0.2 is shown in figure 22.

### Output

Wing weight as a function of the ratio of structural chord to total chord is shown in figure 23. The wing weight estimated by ACSYNT is 789 pounds. PDCYL matches this wing weight when the ratio of structural chord to total chord is approximately 0.25. Nonoptimum weight was not considered in this analysis. In order to estimate nonoptimum weight, nonoptimum factors would need to be recomputed for this type of aircraft.

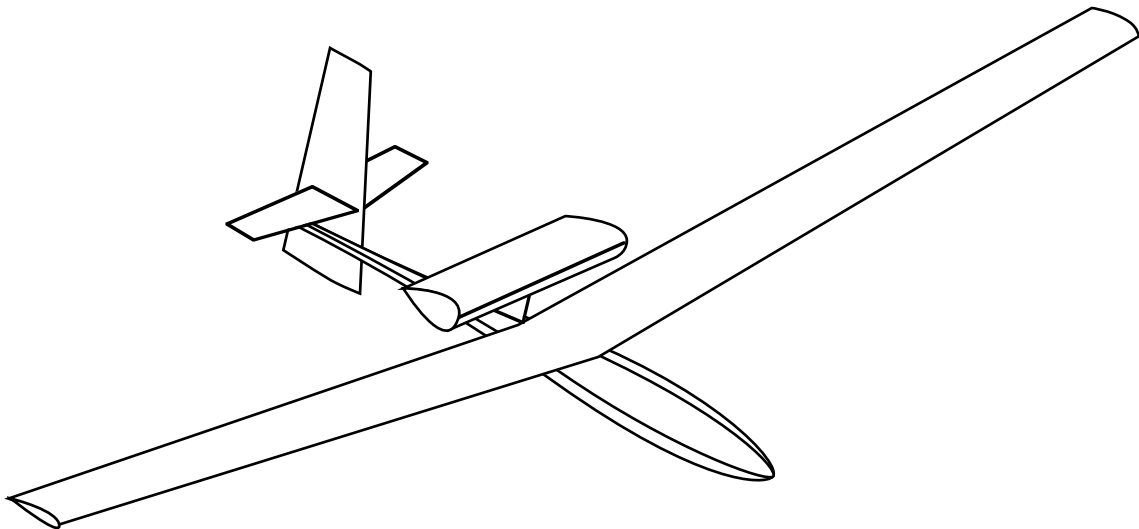


Figure 20. Strato7 configuration.



```

$ADDET ICOD=1, IPLOT=1, NALF=10, NMDTL=10,
  ALIN= -6.8, 0.0, 1.0, 2.0, 4.0, 6.0, 8.0, 10.0, 12.0, 14.0,
  ALTV = 22740.,37475.,50131.,61224.,71097.,79992.,86129.,90000.,
  SMN = 0.085, 0.119, 0.161, 0.210, 0.266, 0.328, 0.379, 0.400,
  ISTRS= 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  ITB= 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  ITS= 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
  $END
$ADRAG CDBMB=10*0.0,
  CDEXTR=10*0.0,
  CDTNK=10*0.00,
  $END
$ATAKE DELFLD=0.0, DELFTO=0.0, DELLED=0.0, DELLTO=0.0, ALFROT=8.0, $END
$APRINT KERROR=2, $END
Spark Ignition Internal Combustion Engine with Triple Turbocharging
$PCONTR HNOU = 0.,31001.,50131.,79992.,90000.,
  SMNOU = 0.0, 0.085, 0.161, 0.328, 0.400,
  NOUPT = 5, $END
$PENGIN ENGNM = 1, NTPENG = 4, ESZMCH = 0.00,
  ESZALT = 0., XNMAX = 7200.0, HPENG = 115.0,
  SWTENG = 6.0, HCRIT = 90000., FSFC = 1.0,
  $END
$PROP AF = 125.0, BL = 2, CLI = 0.5,
  DPROP = 17.88, FPRW = 0.087437, FTHR = 1.0,
  NTPPRP = 12, PSZMCH = 0.00, PSZALT = 0.,
  $END
$PGEAR GR = 7.43, ETR = .95, FGRW = 0.2476234,
  GRSND = 14.86, $END
$PENGC XLENG = 1.5, RLENG = 1.0, DIA1 = 1.0,
  FT = 0.0, FRPN = 1.0, FRBT = 2.0,
  NBDFT = 0.3, ANACHP = 0., DQ = 0.024,
  $END
TRANSPORT
*** WEIGHTS ***
$OPTS WGTO = 3000.0, KERROR = 2,
  SLOPE(1) = 0.47970, TECHI(1) = 0.85,
  SLOPE(2) = 0.97945, TECHI(2) = 0.85,
  SLOPE(3) = 0.64225, TECHI(3) = 0.85,
  SLOPE(4) = 0.85841, TECHI(4) = 0.85,
  SLOPE(6) = 0.70145, TECHI(6) = 0.85,
  SLOPE(7) = 0.85396,
  SLOPE(8) = 0.55290, TECHI(8) = 0.85,
  SLOPE(9) = 1.89582, TECHI(9) = 0.85,
  SLOPE(10) = 1.49618,
  SLOPE(11) = 0.19543,
  SLOPE(12) = 0.48091,
  SLOPE(13) = 3.68569,
  SLOPE(16) = 0.02254,
  SLOPE(17) = 1.0,
  KWING = 6,
  KBODY = 3,
  $END
$FIXW WE = 757.5,
  WFEQ = 0.,
  WFS = 0.,
  WPL = 0.,
  $END

```

Figure 21. Concluded.

\$PDCYLIN

PS=1., TMGW=.05, EFFW=.605,  
EFFC=1.108, ESW=12.9E06, FCSW=75000., DSW=0.058,  
KDEW=1.0, KDFW=1.0,  
ISTAMA=2, CS1=0.01, CS2=0.75,  
  
CLAQR=.001, IFUEL=1, CWMAN=1.0, CF=6.25E-05,  
  
CKF=5.24, EC=2.00, KGC=.368, KGW=.505,  
  
FTST = 4\*58500.,8\*0., FTSB = 4\*58500.,8\*0.,  
FCST = 4\*54000.,8\*0., FCSB = 4\*54000.,8\*0.,  
EST = 4\*10.70E06,8\*0., ESB = 4\*10.70E06,8\*0.,  
EFT = 4\*30.0E06,8\*0., EFB = 4\*30.0E06,8\*0.,  
DST = 4\*.101,8\*0., DSB = 4\*.101,8\*0.,  
DFT = 4\*.292,8\*0., DFB = 4\*.292,8\*0.,  
TMGT = 4\*.03,8\*0., TMGB = 4\*.03,8\*0.,  
KDE=0.9, KDF=0.8,  
CLBR1=1.1, ICYL = 1,  
  
KCONT = 12\*4, KCONB = 12\*4,  
  
AXAC=0., CBUM=1.0, CLAN=0.93,  
CMAN=1.0, ILOAD=3, PGB = 12\*11.5, PGT = 12\*11.5,  
WFBUMP=0.001, WFLAND=0.9,  
  
WTFF=0.07,  
  
VSINK=10.0, STROKE=1.0, CLRG1=.395, CLRG2=0.5,  
WFGR1=0.0031, WFGR2=0.0058, IGEAR=1, GFRL=0.001,  
CLRGW1=0.20, CLRGW2 = 0.0,  
  
ITAIL=1,  
  
ISCHRENK=1, ICOMND=1, WGNO=1.00, SLFMB=1.2,  
WMIS=0., WSUR=0., WCW=1.0, WCA=0.0,  
NWING=40,

\$END

Figure 22. PDCYLIN namelist input for Strato7.

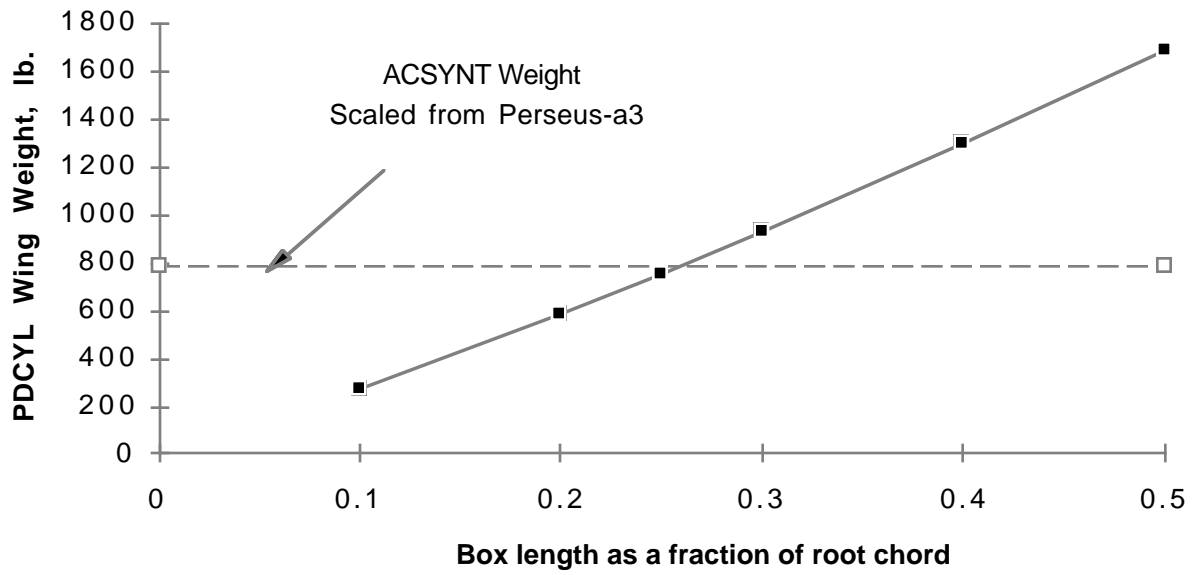


Figure 23. Strato7 wing weight as a function of structural box length.

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| <b>13. ABSTRACT (Maximum 200 words)</b><br><br>A method of estimating the load-bearing fuselage weight and wing weight of transport aircraft based on fundamental structural principles has been developed. This method of weight estimation represents a compromise between the rapid assessment of component weight using empirical methods based on actual weights of existing aircraft, and detailed, but time-consuming, analysis using the finite element method. The method was applied to eight existing subsonic transports for validation and correlation. Integration of the resulting computer program, PDCYL, has been made into the weights-calculating module of the AirCRAFT SYNThesis (ACSYNT) computer program. ACSYNT has traditionally used only empirical weight estimation methods; PDCYL adds to ACSYNT a rapid, accurate means of assessing the fuselage and wing weights of unconventional aircraft. PDCYL also allows flexibility in the choice of structural concept, as well as a direct means of determining the impact of advanced materials on structural weight.<br><br>Using statistical analysis techniques, relations between the load-bearing fuselage and wing weights calculated by PDCYL and corresponding actual weights were determined. A User's Manual and two sample outputs, one for a typical transport and another for an advanced concept vehicle, are given in the appendices. |   |   |                                   |
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